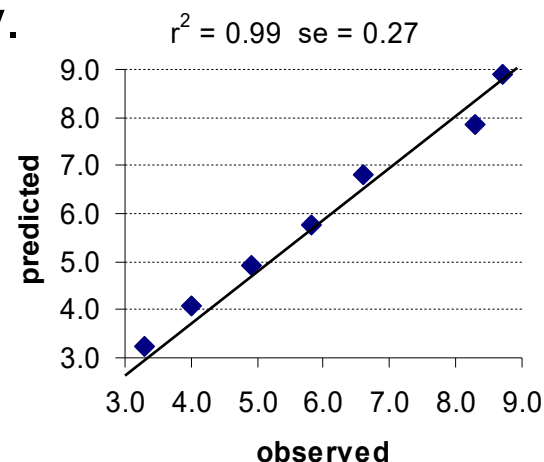


QSAR, QSPR, statistics, correlation, similarity & descriptors

The tools of trade for the computer based *rational drug design*, particularly if there is no structural information about the *target* (protein) available.

QSAR equations form a quantitative connection between chemical structure and (biological) activity.

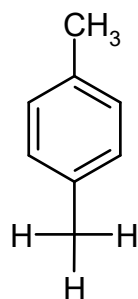
$$\log(1/C) = k_1 \cdot P_1 + k_2 \cdot P_2 + \dots + k_n \cdot P_n$$



The presence of experimentally measured data for a number of known compounds is required, e.g. K_i or IC_{50} values taken from assays.

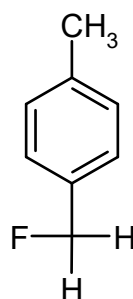
Introduction to QSAR (I)

Suppose we have experimentally determined the binding constants for the following compounds

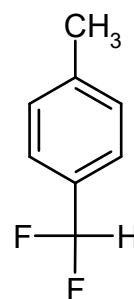


K_i [10^{-9} mol l^{-1}]

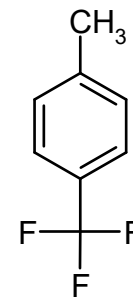
1550



250



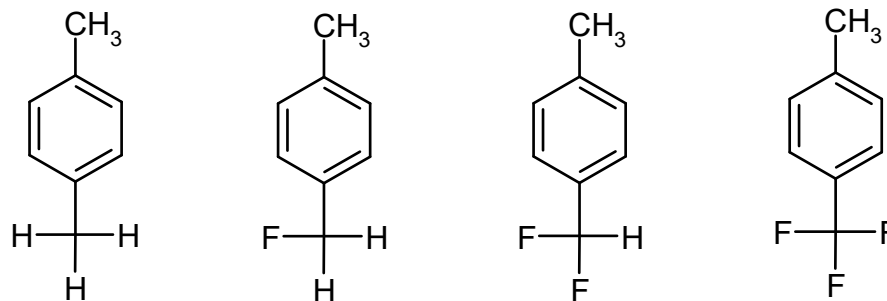
5.0



2.0

Which feature/property is responsible for binding?

Introduction to QSAR (II)



K_i [10^{-9} mol l⁻¹]

1550

250

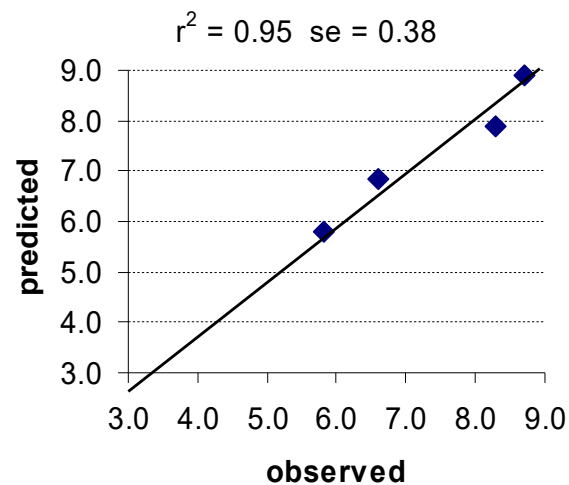
5.0

2.0

Using the number of fluorine atoms as descriptor we obtain following linear regression equation:

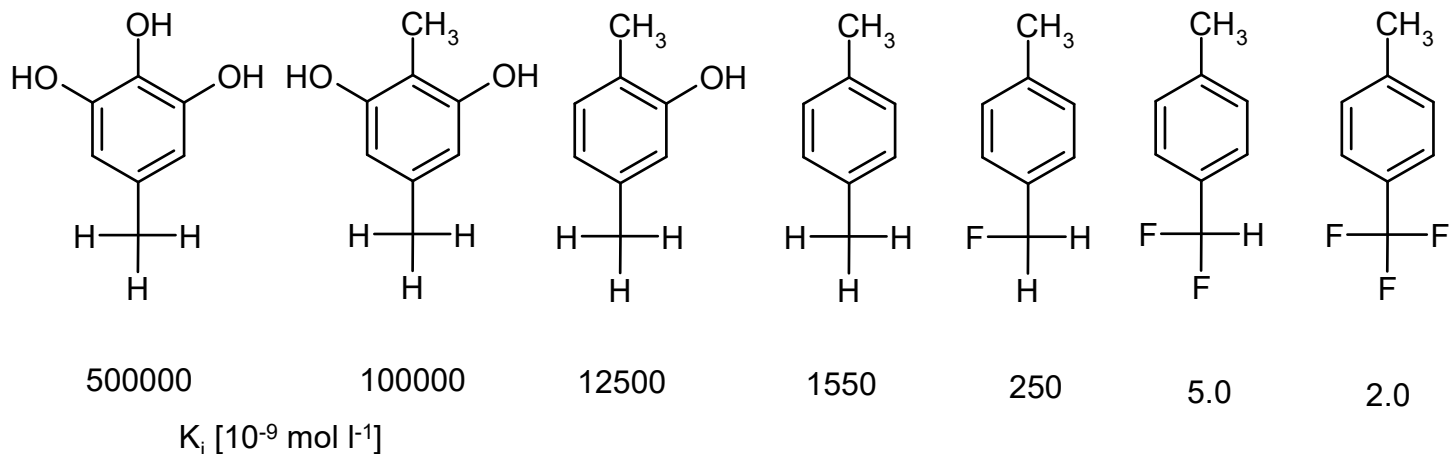
$$\log(1/K_i) = a \cdot n_{\text{fluorine}} + b$$

$$\log(1/K_i) = 1.037 \cdot n_{\text{fluorine}} + 5.797$$



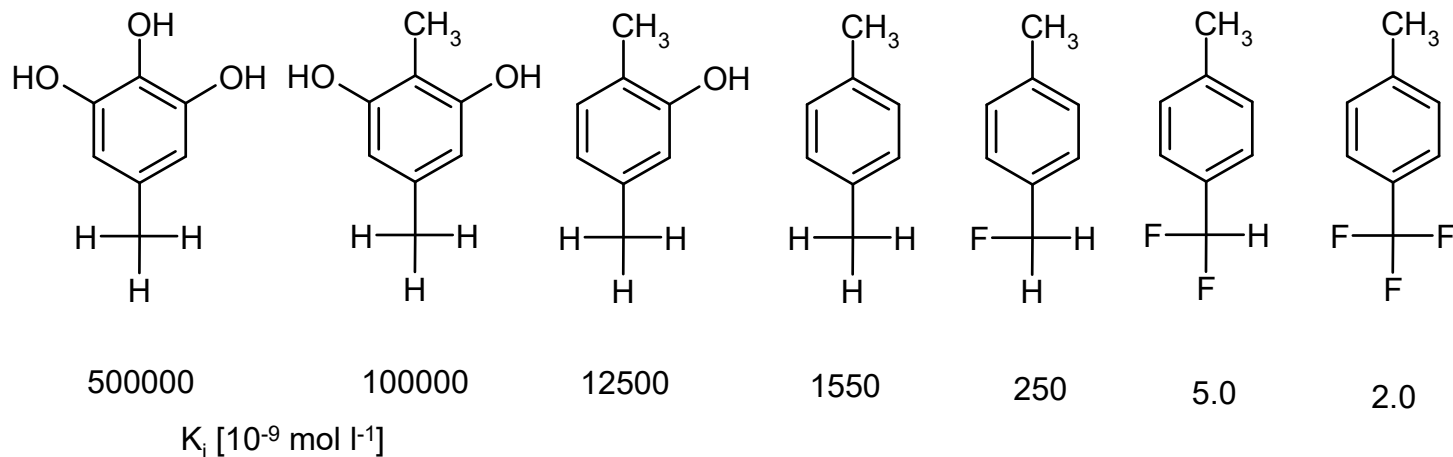
Introduction to QSAR (III)

Now we add some additional compounds



Which features/properties are now responsible for binding?

Introduction to QSAR (IV)

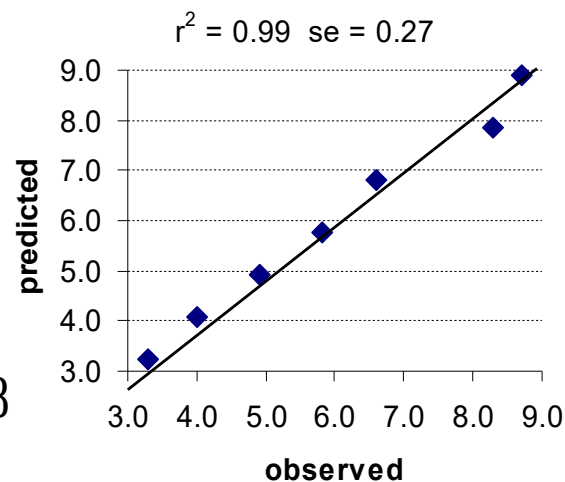


We assume that following descriptors play a major role:

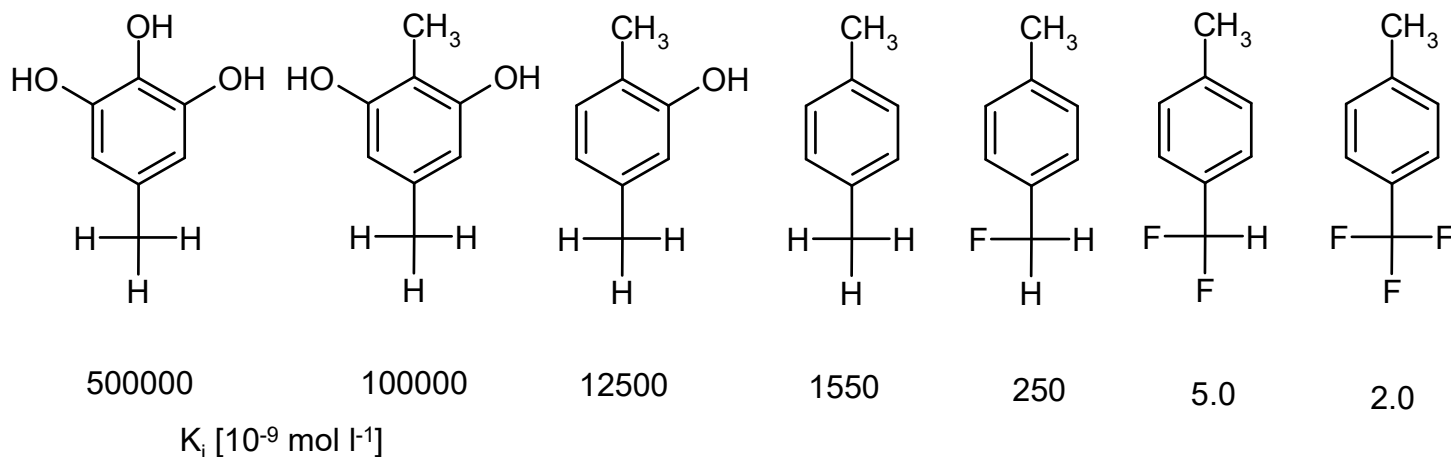
- number of fluorine atoms
- number of OH groups

$$\log(1/K_i) = a_1 \cdot n_{\text{fluorine}} + a_2 \cdot n_{\text{OH}} + b$$

$$\log(1/K_i) = 1.049 \cdot n_{\text{fluorine}} - 0.843 \cdot n_{\text{OH}} + 5.768$$



Introduction to QSAR (V)



$$\log(1/K_i) = 1.049 \cdot n_{\text{fluorine}} - 0.843 \cdot n_{\text{OH}} + 5.768$$

$$r^2 = 0.99 \quad se = 0.27$$

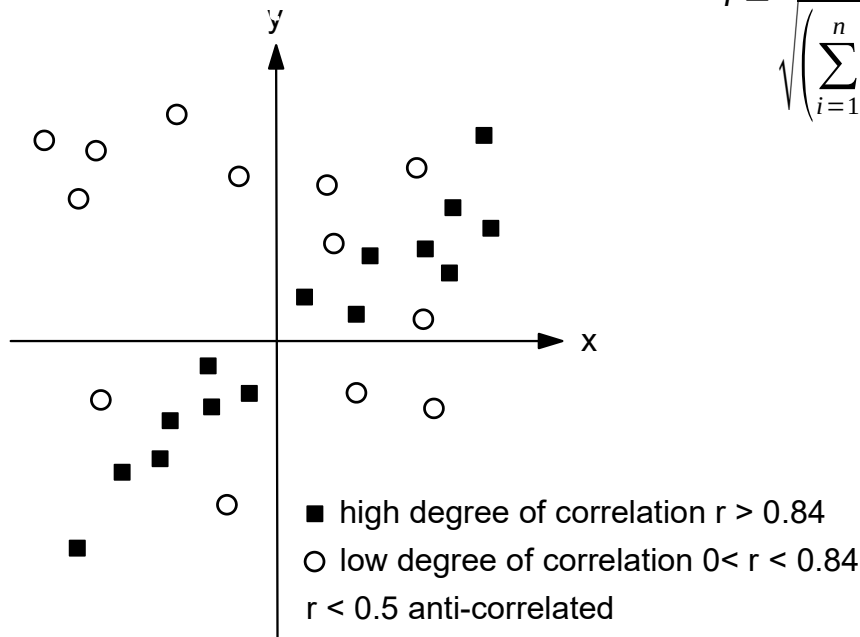
Is our prediction sound or just pure coincidence/random?

→ We will need statistical proof of our assumption
(e.g. using a test set, χ^2 -test, p -values, cross-validation, boots trapping, ...)

Correlation (I)

The most frequently used value is
Pearson's correlation coefficient

$$r = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\left(\sum_{i=1}^n (x_i - \bar{x})^2\right)\left(\sum_{i=1}^n (y_i - \bar{y})^2\right)}} \in [-1 \dots 1]$$



→ A plot tells more than pure numbers!
distribution of the data points, trends, potential outliers,
indication of non-linear correlation...

Definition of terms

QSAR: quantitative structure-activity relationship

QSPR: quantitative structure-property relationship

activity and property can be for example:

$\log(1/K_i)$ K_i constant of binding

$\log(1/IC_{50})$ IC_{50} concentration that produces 50% effect

also physical quantities, such as boiling point, solubility, ...
can be addressed.

aim: prediction of molecular properties from their structure
without the need to perform the experiment.

→ *in silico* instead of *in vitro* or *in vivo*

advantages: saves time and resources

Development of QSAR methods over time (I)

1868 A.C.Brown, T.Fraser:
Physiological activity is a function of the chemical constitution (composition)

but: An absolute direct relationship is not possible, only by using differences in activity of already measured compounds.

remember:

1865 Suggestion for the structure of benzene by A. Kekulé. The chemical structure of most organic compounds at that time was still unknown!

1893 H.H.Meyer, C.E.Overton
The toxicity of organic compounds is related to their partition between aqueous and lipophilic biological phase.

Development of QSAR method over time (II)

1868 E.Fischer
Key and lock principle for enzymes. Again no structural information about enzymes was available!

1930-40 Hammet equation: reactivity of compounds
physical, organic, theoretic chemistry

1964 C.Hansch, J.W.Wilson, S.M.Free, F.Fujita
birth of modern QSAR-methods
Hansch analysis and **Free-Wilson analysis**

$$\log(1/C) = k_1 \cdot P_1 + k_2 \cdot P_2 + \dots + k_n \cdot P_n$$

coefficients (constant) descriptors or variables

linear free energy-related approach

Descriptors

Approaches that form a mathematical relationship between numerical quantities (descriptors P_i) and the physico-chemical properties of a compound (e.g. biological activity $\log(1/C)$), are called QSAR or QSPR, respectively.

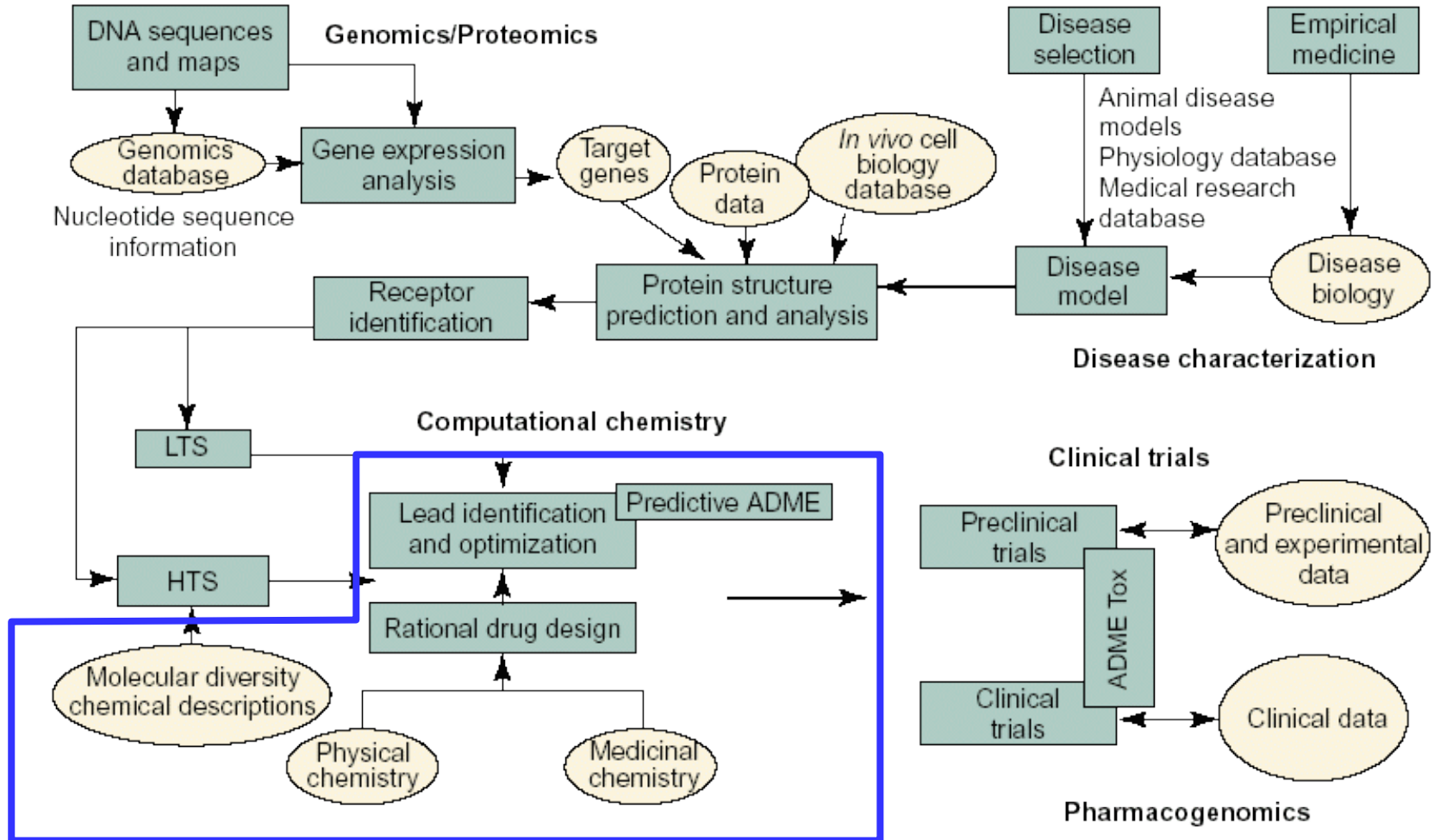
$$\log(1/C) = k_1 \cdot P_1 + k_2 \cdot P_2 + \dots + k_n \cdot P_n$$

Furthermore, descriptors are used to quantify molecules in the context of diversity analysis and in combinatorial libraries.

In principle any molecular or numerical property of the compound can be used as descriptors.

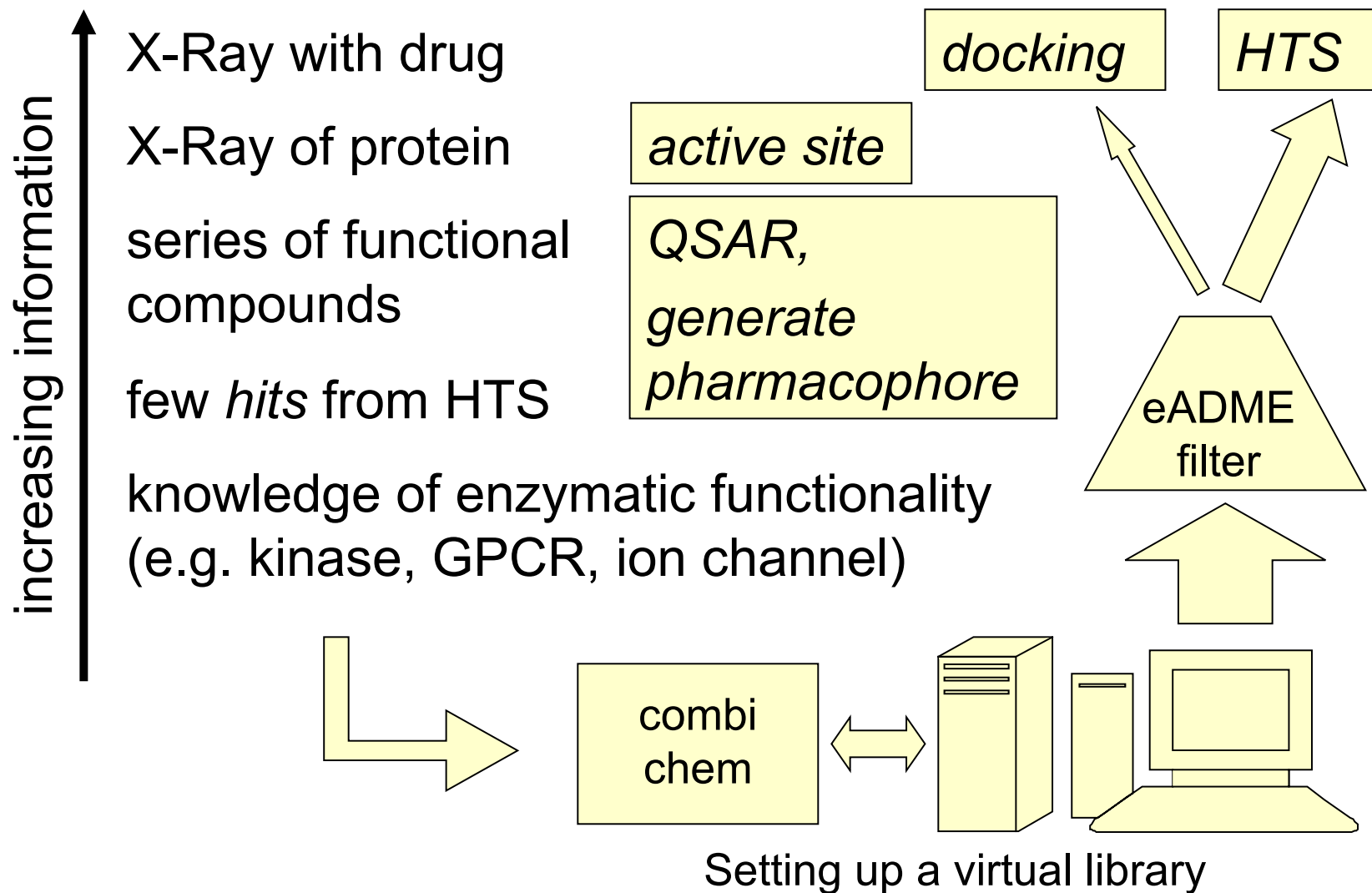
More about descriptors and their classification see <http://www.codessa-pro.com/descriptors/index.htm>

Flow of information in a *drug discovery pipeline*



Drug Discovery Today

Compound selection



(Some) descriptors based on molecular properties used to predict ADME properties

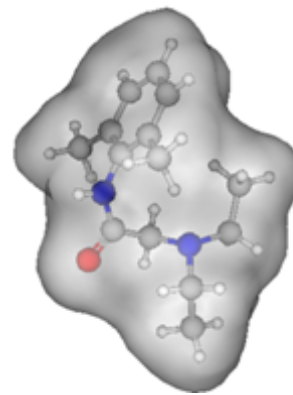
logP water/octanol partitioning coefficient

Lipinski's rule of five

topological indices

polar surface area

similarity / dissimilarity



PubChem Name	WPI-1 Name	WPI-2 Name	WPI-3 Name	WPI-4 Name	WPI-5 Name	WPI-6 Name	WPI-7 Name	WPI-8 Name	WPI-9 Name	WPI-10 Name
1	0.0	14.87141	2.02070	4.0	0.12661	0.026788	1.0264206	0.0	0.0	0.0
2	0.0	36.01443	1.94524	6.10403	-0.04742	NA	NA	0.0	0.0	0.0
3	0.0	8.69480	1.77904	3.32193	-0.00000	0.0	0.0	0.0	0.0	0.0
4	1.0	8.69480	1.77904	3.32193	-0.00000	0.0	0.0	0.0	0.0	0.0
5	0.0	20.05043	2.00042	4.32193	-0.01102	0.0264206	1.0401940	0.0	0.0	0.0
6	1.0	6.47131	1.71782	3.0	-0.04742	0.0	0.0	0.0	0.0	0.0
7	0.0	19.32796	1.94524	4.32193	-0.01742	0.0264206	0.0202111	0.0	0.0	0.0
8	0.0	14.87141	1.81235	4.0	-0.00000	0.0	0.0	0.0	0.0	0.0
9	0.0	14.87141	1.94524	6.07050	-0.00000	1.0264206	1.0401940	0.0	0.0	0.0
10	0.0	8.69480	1.77904	3.32193	-0.00000	0.0	0.0	0.0	0.0	0.0
11	1.0	6.47131	1.71782	3.0	-0.00000	0.0	0.0	0.0	0.0	0.0
12	1.0	17.30217	1.91135	4.10403	-0.07062	0.0264206	0.0264206	0.0	0.0	0.0
13	0.0	14.0625	1.75943	4.0	0.0	0.0	0.0	0.0	0.0	0.0
14	0.0	12.47046	1.81042	3.00705	-0.00000	0.0	0.0	0.0	0.0	0.0
15	0.0	10.52046	1.75943	3.00042	-0.00000	0.0	0.0	0.0	0.0	0.0
16	0.0	10.82046	1.80042	3.00042	-0.00000	0.0	0.0	0.0	0.0	0.0
17	0.0	10.54046	1.75042	3.01042	-0.00000	0.0	0.0	0.0	0.0	0.0
18	1.0	14.81135	1.80042	4.0	0.0	-0.125	0.0264206	0.0	0.0	0.0
19	0.0	18.32796	1.94524	4.32193	-0.14000	0.0	0.0264206	0.0	0.0	0.0
20	0.0	10.87131	1.77904	3.00042	-0.00000	0.0	0.0	0.0	0.0	0.0
21	1.0	8.69480	1.77904	3.32193	-0.00000	0.0	0.0	0.0	0.0	0.0
22	0.0	14.0625	1.75943	4.0	0.0	0.0	0.0	0.0	0.0	0.0
23	0.0	11.8125	1.80042	3.00042	-0.00110	0.0	0.0	0.0	0.0	0.0
24	0.0	36.70443	1.94524	6.10403	-0.00000	0.0264206	0.0264206	0.0	0.0	0.0
25	1.0	12.29046	1.76471	3.00705	-0.00000	0.0	0.0	0.0	0.0	0.0

QSAR quantitative structure activity relationship

QSPR quantitative structure property rel.

„1D“ descriptors (I)

For some descriptors we need only the information that can be obtained from sum formula of the compound. Examples:

molecular weight, total charge, number of halogen atoms, ...

Further 1-dimensional descriptors are obtained by the summation of atomic contributions. Examples:

sum of the atomic polarizabilities

refractivity (*molar refractivity, M_R*)

$$M_R = (n^2 - 1) MW / (n^2 + 2) d$$

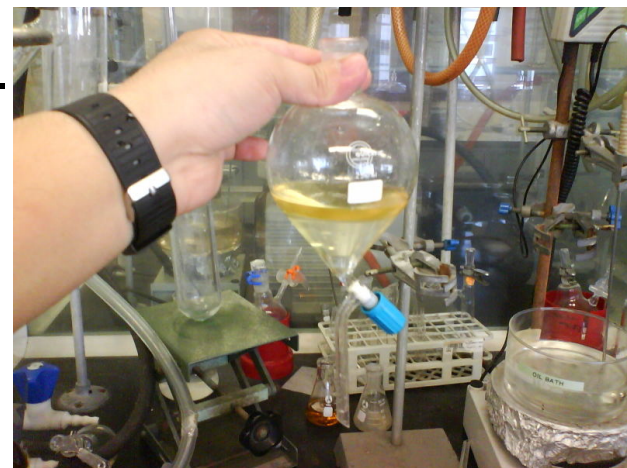
with refractive index n , density d , molecular weight MW

Depends on the polarizability and moreover contains information about the molecular volume (MW / d)

logP (I)

The *n*-octanol / water partition coefficient, respectively its logarithmic value is called logP.

Frequently used to estimate the membrane permeability and the bioavailability of compounds, since an orally administered drug must be enough **lipophilic** to cross the lipid bilayer of the membranes, and on the other hand, must be **sufficiently water soluble** to be transported in the blood and the lymph.



hydrophilic $-4.0 < \log P < +8.0$ lipophilic

glucose -3.24

flurbiprofene $+4.16$

„typical“ drugs < 5.0

logP (II)

An increasing number of methods to predict logP have been developed:

Based on molecular fragments (atoms, groups, and larger fragments)

ClogP Leo, Hansch et al. *J.Med.Chem.* **18** (1975) 865.
problem: non-parameterized fragments
(occur up to 25% of all compounds in substance libraries)

Based on atom types (similar to force field atom types)

SlogP S.A. Wildman & G.M.Crippen *J.Chem.Inf.Comput.Sci.*
39 (1999) 868.

AlogP, MlogP, XlogP...

Parameters for each method were obtained using a mathematical fitting procedure (linear regression, neural net,...)

Review: R.Mannhold & H.van de Waaterbeemd,
J.Comput.-Aided Mol.Des. **15** (2001) 337-354.

logP (III)

Further logP prediction methods apply whole molecule properties, such as

- molecular surface (polar/non-polar area, or their electrostatic properties = electrostatic potential)
- dipole moment and molecular polarizability
- ratio of volume / surface (globularity)

Example: Neural net trained with quantum chemical data

logP T. Clark et al. *J.Mol.Model.* **3** (1997) 142.

„1D“ descriptors (II)

Further atomic descriptors use information based on empirical atom types like in force fields. Examples:

- Number of halogen atoms
- Number of sp^3 hybridized carbon atoms
- Number of H-bond acceptors (N, O, S)
- Number of H-bond donors (OH, NH, SH)
- Number of aromatic rings
- Number of COOH groups
- Number of ionizable groups (NH_2 , COOH)
- ...
- Number of freely rotatable bonds (single bonds that are not in a ring)

Fingerprints as binary descriptors

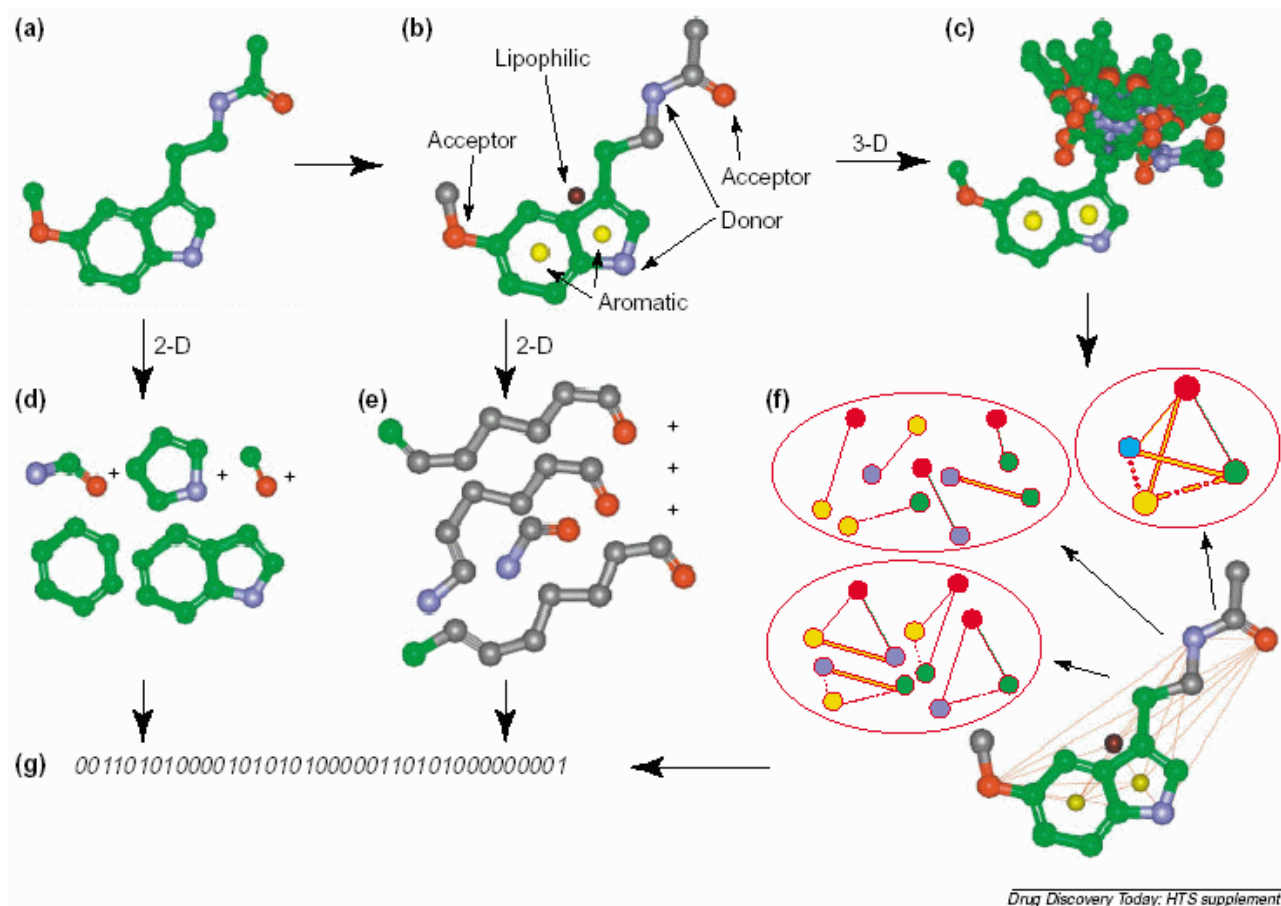


Figure 2. Schematic illustration of primary methods used in molecular fingerprint creation. **(a)** Create 2-D and 3-D model of molecule; **(b)** deconstruct the molecule into pharmacophoric elements; **(c)** generate conformational models; **(d)** deconstruct the molecule into topological/substructural elements; **(e)** determine distance between pharmacophoric groups using bond counts; **(f)** determine 2-, 3- or 4-center distance combinations of pharmacophoric groups for each conformer; and **(g)** determine the presence or absence of each descriptor element and combine to create a binary fingerprint.

Lipinski's Rule of 5

Combination of descriptors to estimate intestinal absorption.
Insufficient uptake of compounds, if

Molecular weight > 500

slow diffusion

$\log P > 5.0$

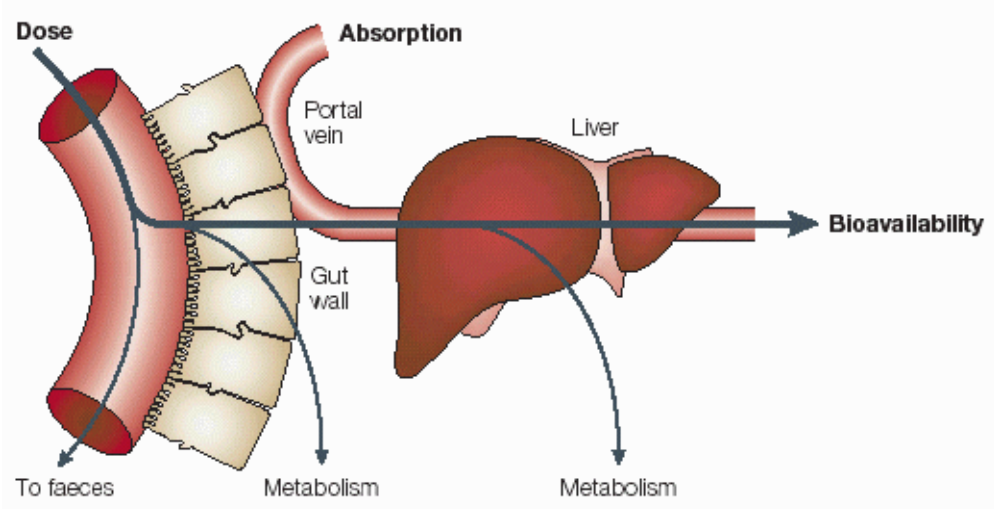
too lipophilic

> 5 H-bond donors (OH and NH)

to many H-bonds with the head

>10 H-bond acceptors (N and O atoms)

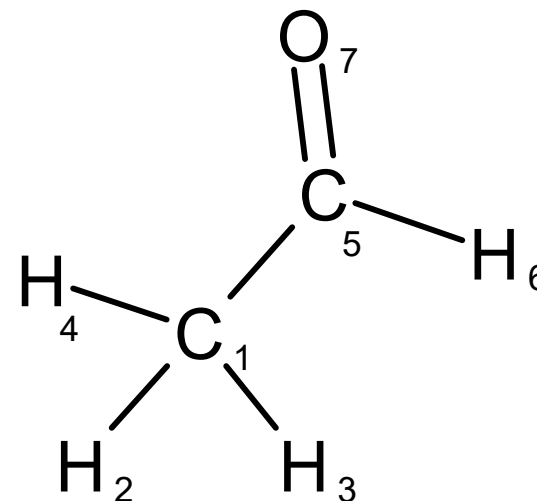
groups of the membrane



C.A. Lipinski et al. *Adv. Drug. Delivery Reviews* **23** (1997) 3.

2D descriptors (I)

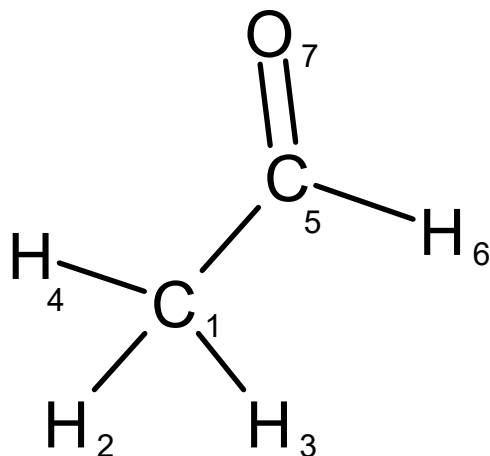
Descriptors derived from the configuration of the molecules (covalent bonding pattern) are denoted **2D descriptors**. Since no coordinates of atoms are used, they are in general **conformationally independent**, despite containing topological information about the molecule. C.f. representation by SMILES



	adjacency matrix M					distance matrix D								
C1	0	1	1	1	1	0	0	0	1	1	1	1	2	2
H2	1	0	0	0	0	0	0	1	0	2	2	2	3	3
H3	1	0	0	0	0	0	0	1	2	0	2	2	3	3
H4	1	0	0	0	0	0	0	1	2	2	0	2	3	3
C5	1	0	0	0	0	1	1	1	2	2	2	0	1	1
H6	0	0	0	0	1	0	0	2	3	3	3	1	0	2
O7	0	0	0	0	1	0	0	2	3	3	3	1	2	0

2D descriptors (II)

The essential topological properties of a molecule are the degree of branching and the molecular shape.



An sp^3 hybridized carbon has got 4 valences, an sp^2 carbon only 3.

Thus the ratio of the actual branching degree to the theoretically possible branching degree can be used as descriptor because it is related to the saturation (double or aromatic bonds where hydrogens can be added). C.f. unsaturated fatty acids

2D descriptors (III)

Common definitions:

Z_i ordinary number (H=1, C=6, N=7, LP=0)

h_i number of H atoms bonded to atom i

d_i number of non-hydrogen atoms bonded to atom i

Descriptors accounting for the degree of branching and the flexibility of a molecule:

Kier & Hall Connectivity Indices

p_i sum of s and p valence electrons of atom i

$v_i = (p_i - h_i) / (Z_i - p_i - 1)$ for all non-hydrogen (heavy) atoms

Kier and Hall Connectivity Indices

Z_i ordinary number (H=1, C=6, LP=0)

d_i number of heavy atoms bonded to atom i

p_i number of s and p valence electrons of atom i

$v_i = (p_i - h_i) / (Z_i - p_i - 1)$ for all heavy atoms

Chi0 0th order $\chi_0 = \sum_i \frac{1}{\sqrt{d_i}}$ for all heavy atom with $d_i > 0$

Chi1 1st order $\chi_1 = \sum_i \sum_{\substack{j>i \\ i \text{ is bonded to } j}} \frac{1}{\sqrt{d_i d_j}}$ for all heavy atoms if

Chi0v Valence index $\chi_{0v} = \sum_i \frac{1}{\sqrt{v_i}}$ for all heavy atoms with $v_i > 0$

Kier and Hall Shape Indices (I)

n number of heavy atoms (non-hydrogen atoms)

m total number of bonds between all heavy atoms

p_2 number of paths of length 2

p_3 number of paths of length 3 from the distance matrix **D**

$$\text{Kappa1} \quad \kappa_1 = \frac{n(n-1)^2}{m^2}$$

$$\text{Kappa2} \quad \kappa_2 = \frac{(n-1)(n-2)^2}{p_2^2}$$

$$\text{Kappa3} \quad \kappa_3 = \frac{(n-1)(n-3)^2}{p_3^2} \text{ for even } n$$

$$\kappa_3 = \frac{(n-3)(n-2)^2}{p_3^2} \text{ for odd } n$$

Kier and Hall Shape Indices (II)

Relating the atoms to sp^3 -hybridized carbon atoms yields the Kappa alpha indices

$$\alpha = \sum_i^n \frac{r_i}{r_c - 1}$$

r_i covalence radius of atom i
 r_c covalence radius of an sp^3 carbon atom

$$\kappa_{\alpha 1} = \frac{s(s-1)^2}{(m+\alpha)^2} \text{ with } s = n + \alpha$$

element	hybridization	α
C	sp^3	0
C	sp^2	-0.13
C	sp	-0.22
N	sp^3	-0.04
N	sp^2	-0.20
N	sp	-0.29
O	sp^3	-0.04
P	sp^3	+0.43
S	sp^3	+0.35
Cl		+0.29

Balaban, Wiener, and Zagreb Indices

n number of heavy atoms (non-hydrogen atoms)

m total number of bonds between all heavy atoms

d_i number of heavy atoms bonded to atom i

$w_i = \sum_{i \neq j} D_{ij}$ Sum of the off-diagonal matrix elements of atom i in the distance matrix **D**

BalabanJ
$$\frac{m}{m-n+1} \sum \frac{1}{\sqrt{w_i w_j}}$$

WienerJ (path number) $\frac{1}{2} \sum_i^n w_i$ Correlates with the boiling points of alkanes

Wiener polarity $\frac{1}{2} \sum_i^n w_i$ if $D_{ij} \geq 3$

Zagreb index $\sum_i d_i^2$ for all heavy atoms i

What kind of information do topological indices contain?

topological indices are associated with the

- degree of branching in the molecule
- size and spacial extention of the molecule
- structural flexibility

Usually it is not possible to correlate a chemical property directly by using only one single index.

Although topological indices encode the same properties as fingerprints do, they are harder to interpret, but can be generated numerically more easily.

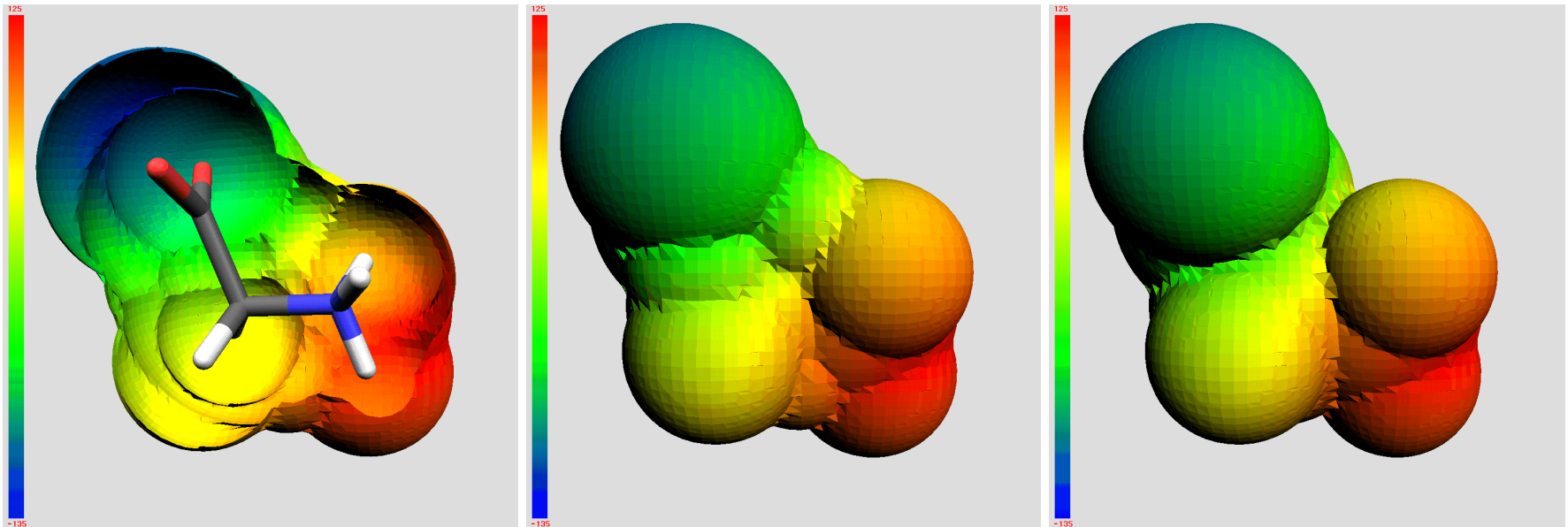
3D descriptors

Descriptors using the atomic coordinates (x,y,z) of a molecule are therefore called **3D descriptors**.

As a consequence they usually **depend on the conformation**.
(rotation around single bonds causes leads to other conformations)

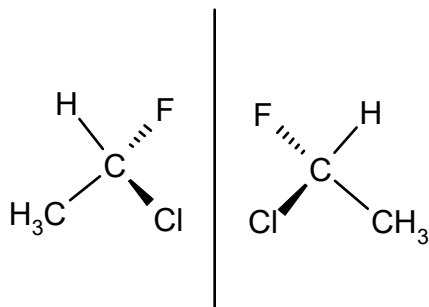
Examples:

van der Waals volume, molecular surface, polar surface, electrostatic potential (ESP), dipole moment



Chirality Descriptors

Most biological interactions are stereospecific e.g. ligand binding



Stereoisomers share identical 1D and 2D-descriptors, because they have the same topology.

Ideas for including chirality:

- Using differences of the van der Waals volume or the electrostatic potential after superposition (rotation)
- Adding +1/-1 to chiral centers in the adjacency matrix while computing topological descriptors
- Modifying the sign of 1D-descriptors (electronegativity, size, polarizability,...) with respect to the enantiomer

Lit: G.M.Crippen *Curr.Comput.-Aided Drug Des.* **4** (2008) 259-264.

Quantum mechanical descriptors (selection)

Atomic charges (*partial atomic charges*) No observables!

Mulliken population analysis, Gasteiger-Marsili charges, electrostatic potential (ESP) derived charges

dipole moment

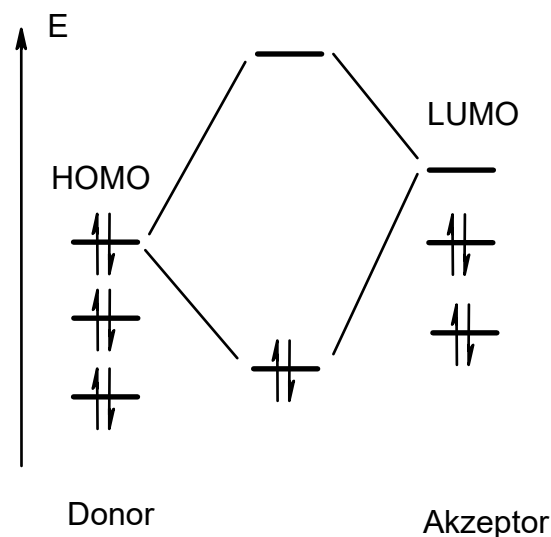
polarizability

HOMO / LUMO

energies of the frontier orbitals
given in eV

covalent hydrogen bond acidity/basicity

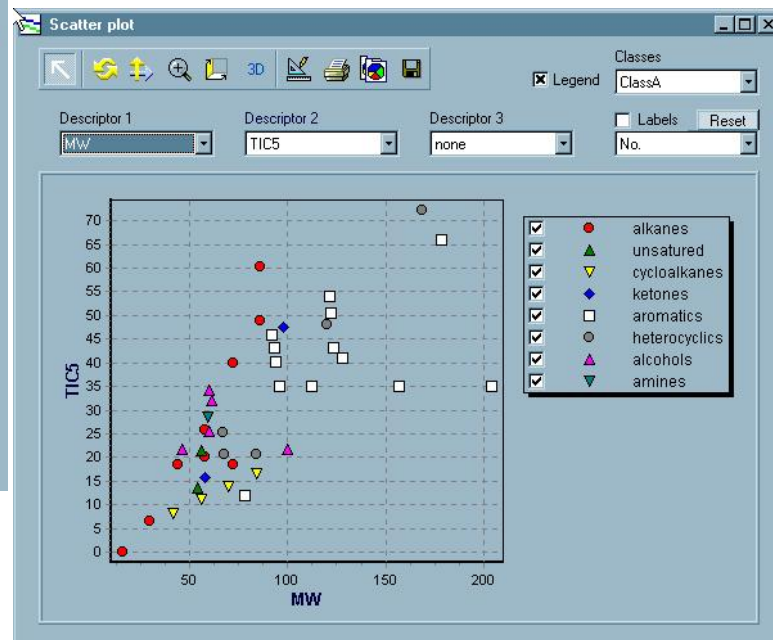
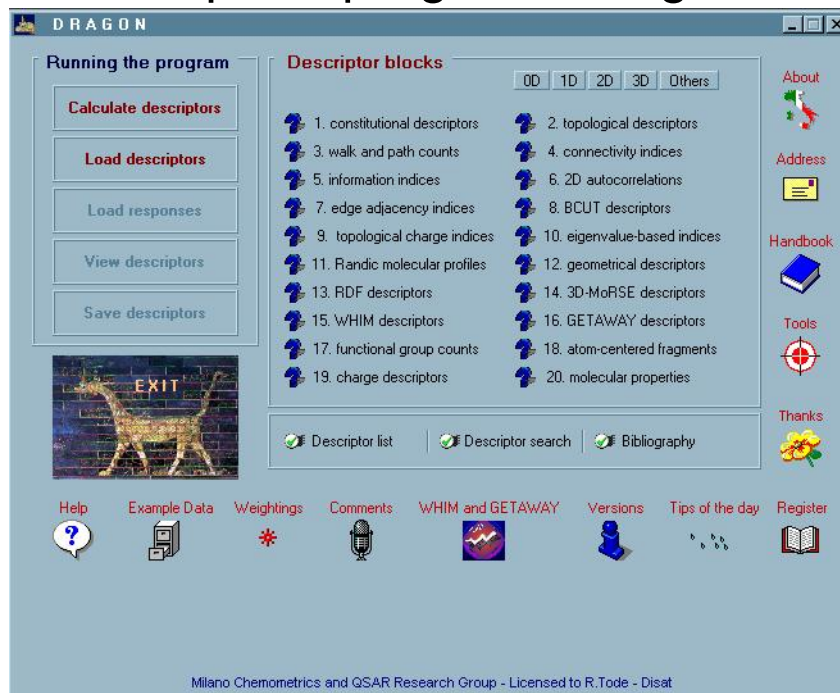
difference of the HOMO/LUMO energies compared to those of water → is the compound a better hydrogen-bond donor/acceptor than a water molecule?



Lit: M. Karelson et al. *Chem.Rev.* **96** (1996) 1027

(e)DRAGON

a computer program that generates >1400 descriptors

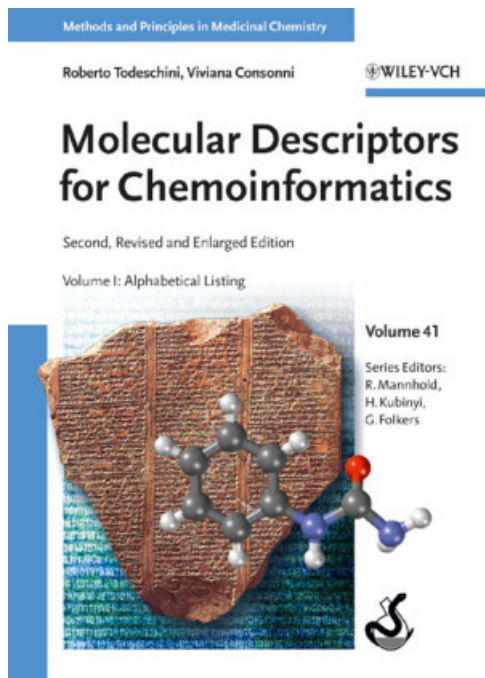


Roberto Todeschini

<http://www.vcclab.org/lab/edragon/>

Requires 3D-structure of molecules as input

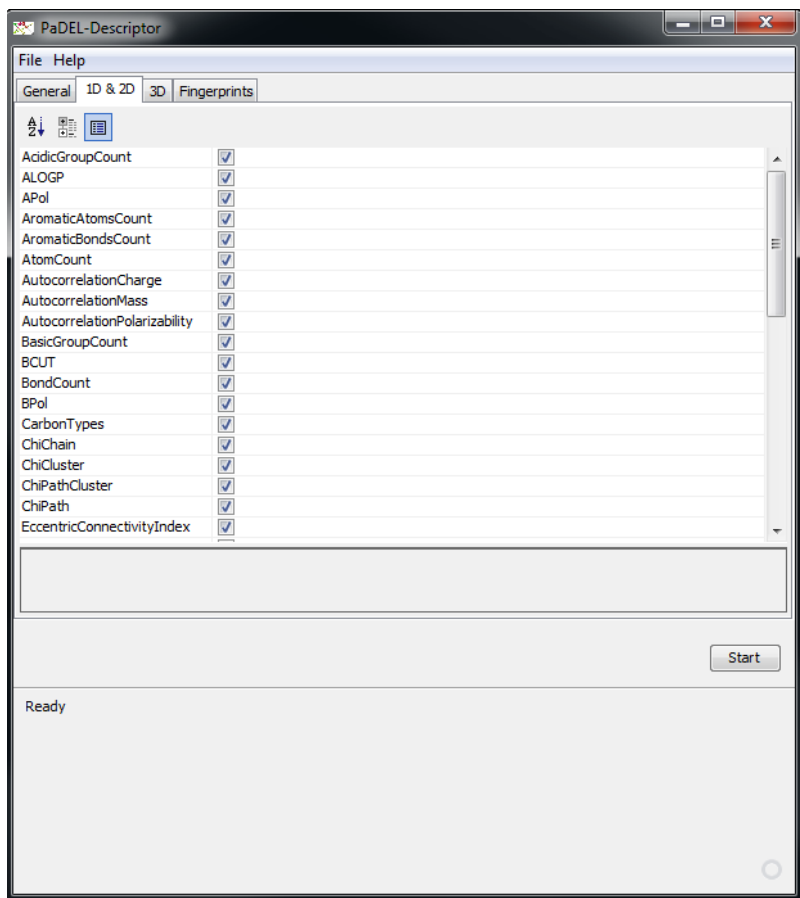
Further information about descriptors



Roberto Todeschini, Viviana Consonni
Handbook of Molecular Descriptors,
Wiley-VCH, 2nd ed. (2009)
1257 pages

CODESSA Alan R. Katritzky, Mati Karelson et al.
<http://www.codessa-pro.com>

PaDEL-Descriptor



```
Administrator: C:\Windows\system32\cmd.exe
C:\padel>java -jar PaDEL-Descriptor.jar -help
usage: java -jar PaDEL-Descriptor.jar
       -waitingjobs <waitingjobs>           Maximum number of jobs to store in
       -threads <threads>                   queue for worker threads to process. Use -
1 to set it to 50*Max threads.             Maximum number of threads to use.
       -threads <threads>                   Use -1 to use as many threads as the numbe
r of cpu cores
       -d                                    Calculate 1D and 2D descriptors
       -2d                                    Calculate 3D descriptors
       -3d                                    Add explicit hydrogen atoms to
       -addhydrogens                         molecules before calculating descriptors
       -config <config>                     Configuration file
       -convert3d                             Convert molecule to 3D
       -descriptortypes <descriptortypes>    Descriptor types file
       -detectaromaticity                    Remove existing aromaticity
       -detectaromaticity                    information and automatically detect aroma
ticity in the molecule before               calculation of descriptors
       -dir <directory>                     Set directory containing structural
files
       -file <file>                          Set file to save calculated
descriptors
       -fingerprints                         Calculate fingerprints
       -help                                  Print this message
       -log                                   Create a log file.
Name of log file is the name of the descri
ptors file with a .log                     extension.
       -maxcpdperfile <maxcpdperfile>       Maximum number of compounds to be
stored in each descriptor file. Use 0 for
unlimited
       -removesalt                           Remove salt from molecule
       -retainorder                          Retain order of molecules in
structural files for descriptor file. This
may lead to large memory use if             descriptor calculations are stuck at one m
olecule as the others will not            be written to file and cleared from memory
       -usefilenameasmolname                 Use filename <minus the extension>
as molecule name
C:\padel>_
```

Open Source Software (JAVA)

Chun Wei Yap

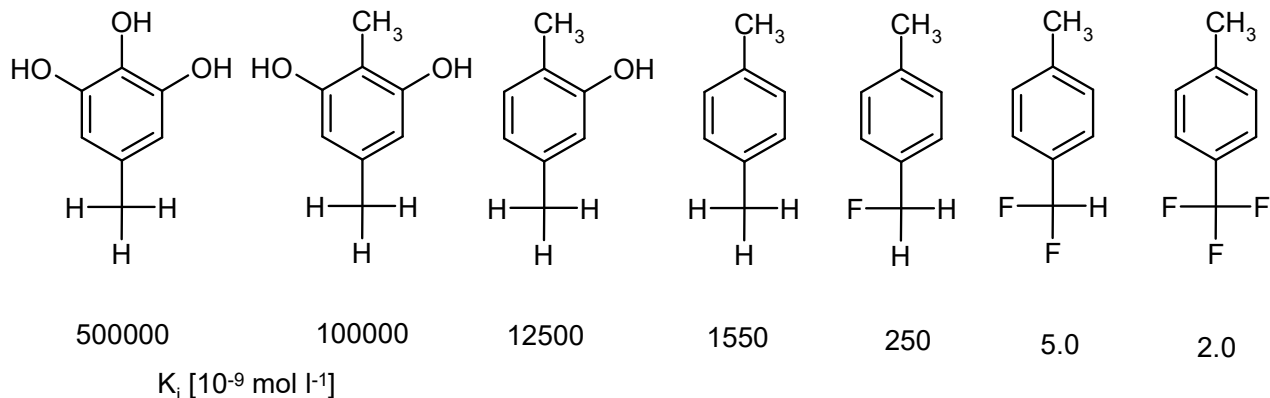
<http://www.yapcwsoft.com/dd/padeldescriptor/>

C.W. Yap *J.Comput.Chem.* **32** (2011) 1466-1474.

Chosing the right compounds (I)

To derive meaningful QSAR predictions we need

- A sufficient number of compounds **statistically sound**
- Structurally diverse compounds **tradeoff between count and similarity**



How similar are chemical compounds to each other?

→ Clustering using distance criteria
that are based on the descriptors

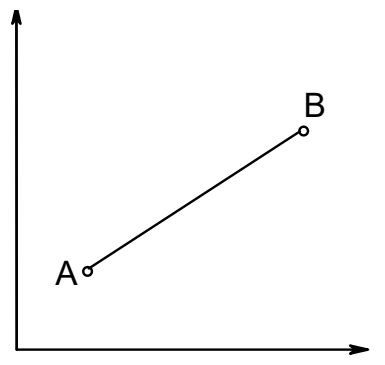
Distance criteria and similarity indices (I)

χ_A fulfilled property of molecule A

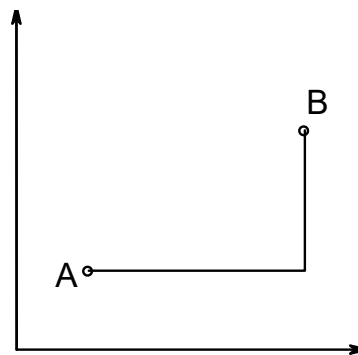
$|\chi_A \cap \chi_B|$ intersection of common properties of A and B

$|\chi_A \cup \chi_B|$ unification of common properties of A and B

Euclidian distance



Manhattan distance



formula

$$D_{A,B} = \sqrt{\sum_{i=1}^N (x_{iA} - x_{iB})^2}$$

$$D_{A,B} = \sum_{i=1}^N |x_{iA} - x_{iB}|$$

definition

$$D_{A,B} = \sqrt{|\chi_A \cup \chi_B| - |\chi_A \cap \chi_B|}$$

$$D_{A,B} = |\chi_A \cup \chi_B| - |\chi_A \cap \chi_B|$$

range

∞ to 0

∞ to 0

other names

—

City-Block, Hamming

Distance criteria and similarity indices (II)

Soergel distance

$$D_{A,B} = \sum_{i=1}^N |x_{iA} - x_{iB}| / \sum_{i=1}^N \max(x_{iA}, x_{iB})$$

$$D_{A,B} = |X_A \cup X_B| - |X_A \cap X_B| / |X_A \cup X_B|$$

1 to 0

–

Tanimoto index

$$S_{A,B} = \left(\sum_{i=1}^N x_{iA} x_{iB} \right) / \left(\sum_{i=1}^N (x_{iA})^2 + \sum_{i=1}^N (x_{iB})^2 - \sum_{i=1}^N x_{iA} x_{iB} \right)$$

$$S_{A,B} = |X_A \cap X_B| / |X_A \cup X_B|$$

–0.333 to +1 (continuous values)

0 to +1 (binary on/off values)

Jaccard coefficient

For binary (dichotomous) values the Soergel distance is complementary to the Tanimoto index

Distance criteria and similarity indices (III)

Dice coefficient

$$S_{A,B} = \left(2 \sum_{i=1}^N x_{iA} x_{iB} \right) / \left(\sum_{i=1}^N (x_{iA})^2 + \sum_{i=1}^N (x_{iB})^2 \right)$$

$$S_{A,B} = 2|X_A \cap X_B| / (|X_A| + |X_B|)$$

-1 to +1

0 to +1

Hodgkin index

Czekanowski coefficient

Sørensen coefficient

monotonic with the
Tanimoto index

Cosinus coefficient

$$S_{A,B} = \left(\sum_{i=1}^N x_{iA} x_{iB} \right) / \sqrt{\sum_{i=1}^N (x_{iA})^2 \cdot \sum_{i=1}^N (x_{iB})^2}$$

$$S_{A,B} = |X_A \cap X_B| / \sqrt{|X_A| |X_B|}$$

0 to +1 (continuous values)

0 to +1 (binary on/off values)

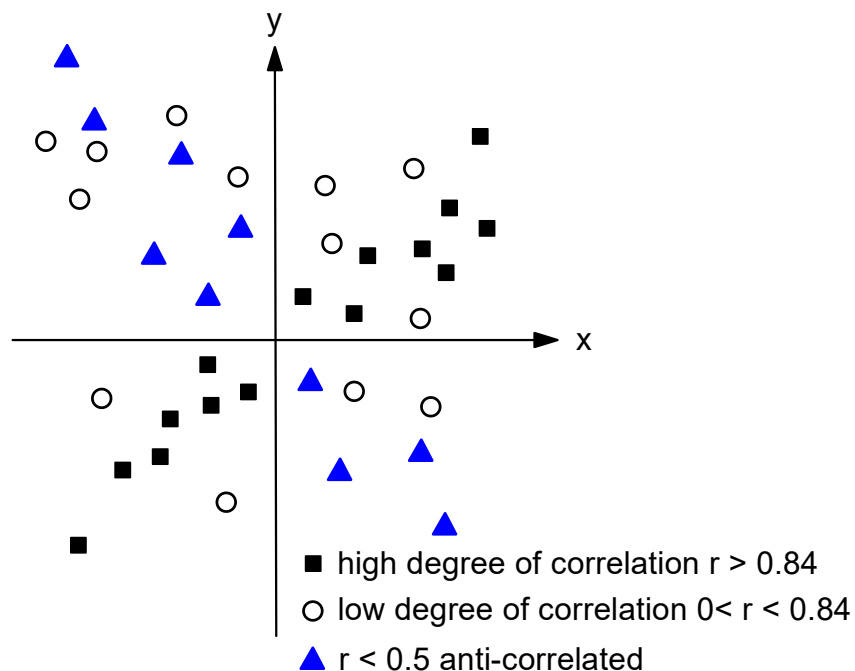
Carbo index

Ochiai coefficient

Highly correlated to the
Tanimoto index

Correlation between descriptors (I)

Descriptors can also be inter-correlated (colinear) to each other
→ redundant information should be excluded



Usually we will have a wealth of descriptors (much more than the available molecules) to choose from. To obtain a reasonable combination in our QSAR equation, multivariate methods of statistics or other selection procedures must be applied.

Correlation between descriptors (II)

How many descriptors can be used in a QSAR equation before overfitting sets in?

Rule of thumb:

per descriptor used, at least 5 molecules (data points) should be present

otherwise the possibility of finding a coincidental correlation is too high (as we will see later).

≥ 10 molecules \rightarrow 2 descriptors

≥ 15 molecules \rightarrow 3 descriptors...

(Ockham's razor: it's possible to fit anything to anything)

Therefore: Principle of parsimony; use the most simple explanation.



William of Ockham (1285 - 1347)

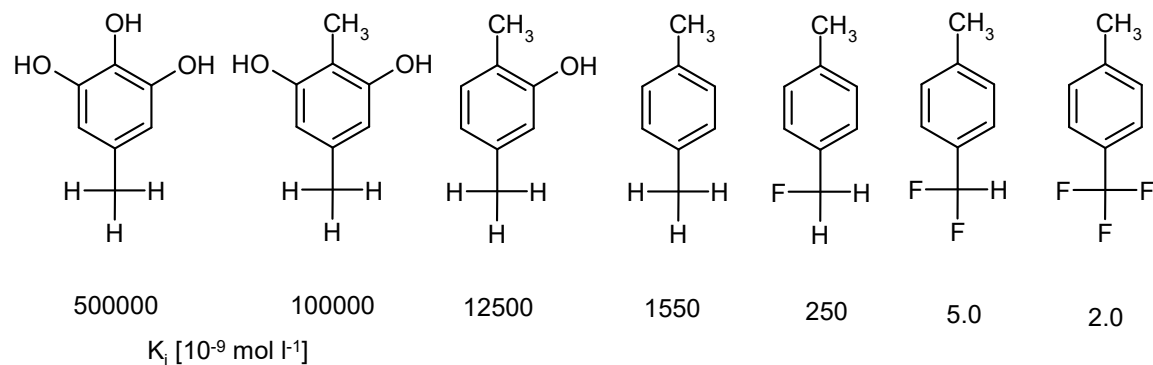
Deriving QSAR equations (I)

After removing the inter-correlated descriptors, we have to determine the coefficients k_i for those descriptors that appear in the QSAR equation.

Such multiple linear regression analysis (*least square fit* of the according coefficients) is performed by statistics programs.

There are several ways to proceed:

1. Using the descriptor that shows the best correlation to the predicted property first and adding stepwise descriptors that yield the best improvement (**forward regression**)



Deriving QSAR equations (II)

2. Using all available descriptors first, and removing stepwise those descriptors that worsen the correlation fewest.
(**backward regression/elimination**)

3. Determining the best combination of the available descriptors for given number of descriptors appearing in the QSAR equation (2,3,4,...) (**best combination regression**)

This is usually not possible due to the exponential runtime.

Problem of forward and backward regression:

Risk of local minima

Problems: Which descriptors are relevant or significant?

Which descriptors are easy to understand?

Determination of such descriptors see lecture 6