V6 – Biological PPI Networks - are they really scale-free? - network growth - functional annotation in the network

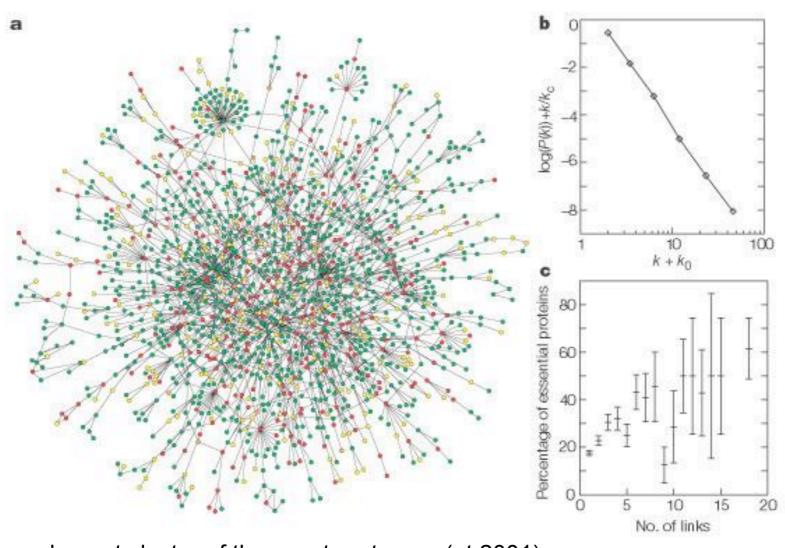
Mon, Nov 16, 2015

brief communications

Lethality and centrality in protein networks

The most highly connected proteins in the cell are the most important for its survival.

Jeong, Mason, Barabási, Oltvai, Nature 411 (2001) 41



→ "PPI networks apparently are scale-free..."

"Are" they scale-free or
"Do they look like" scale-free???

largest cluster of the yeast proteome (at 2001)

Partial Sampling

Estimated for yeast: 6000 proteins, 30000 interactions

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Data set	Ito <i>et al.</i> (yeast)	Uetz <i>et al.</i> (yeast)	Ito-Uetz combined	Li <i>et al</i> . (worm)	Giot <i>et al</i> . (fly)	Minimum value	Maximum value
Total number of nodes	797	1,005	1,417	1,415	4,651	797	4,651
Nodes in main component	417 (52%)	473 (47%)	970 (68%)	1,260 (89%)	3,039 (65%)	47%	89%
Total number of interactions	806	948	1,520	2,135	4,787	806	4,787
Interactions in main component	544	558	1,229	2,038	3,715	544	3,715
R-square	0.843	0.954	0.899	0.885	0.91	0.843	0.954
γ	-1.82	-2.42	-1.91	-1.59	-2.75	-2.75	-1.59
< <i>k</i> >	1.96	1.84	2.15	2.98	2.04	1.84	2.98
Average clustering coefficient	0.2	0.11	0.09	0.09	0.06	0.06	0.2
Number of network components	143	177	160	70	591	70	591
Average component size	5.6	5.7	8.9	20.2	7.9	5.6	20.2
Characteristic path length	6.14	7.48	6.55	4.91	9.43	4.91	9.43
Number of baits	455	512	827	502	2,820	455	2,820

The linear regression R-square measures the linearity between log(n(k)) and log(k) i.e. the fit to a power-law distribution. γ is the exponent of the power law distribution formula that best fits the observed distribution. $\langle k \rangle$ is the average number of interactions per protein observed in the network. For the Ito, Li and Giot data sets only the high confidence interactions were considered (core).

Y2H **covers** only **3...9%** of the complete interactome!

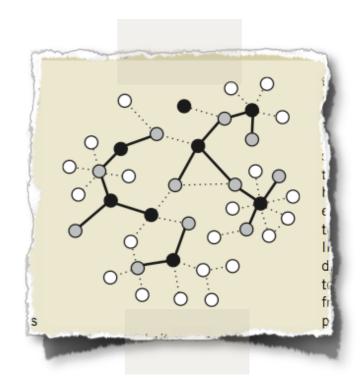
Effect of sampling on topology predictions of protein-protein interaction networks

Jing-Dong J Han¹⁻³, Denis Dupuy^{1,3}, Nicolas Bertin¹, Michael E Cusick¹ & Marc Vidal¹

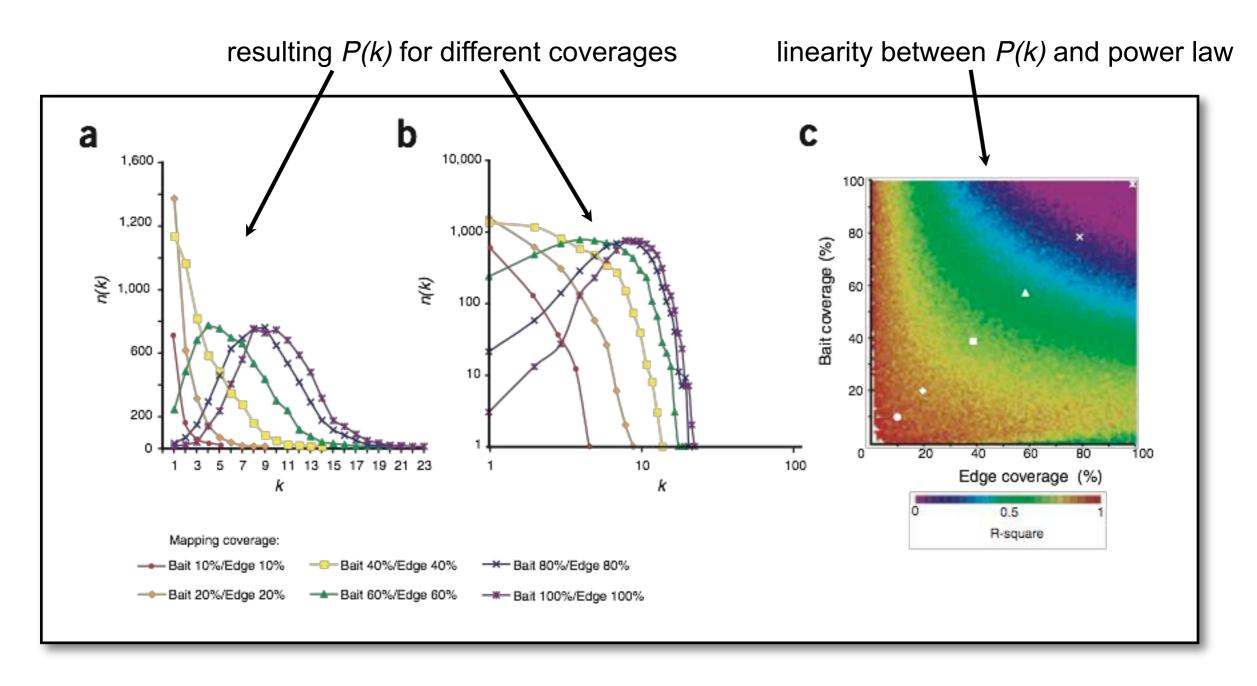
Nature Biotech 23 (2005) 839

Generate networks of various types, sample sparsely from them

- → degree distribution?
- Random (ER / Erdös-Renyi) $\rightarrow P(k)$ = Poisson
- Exponential (EX) $\rightarrow P(k) \sim \exp[-k]$
- scale-free / power-law (PL) $\rightarrow P(k) \sim k^{-\gamma}$
- P(k) = truncated normal distribution (TN)

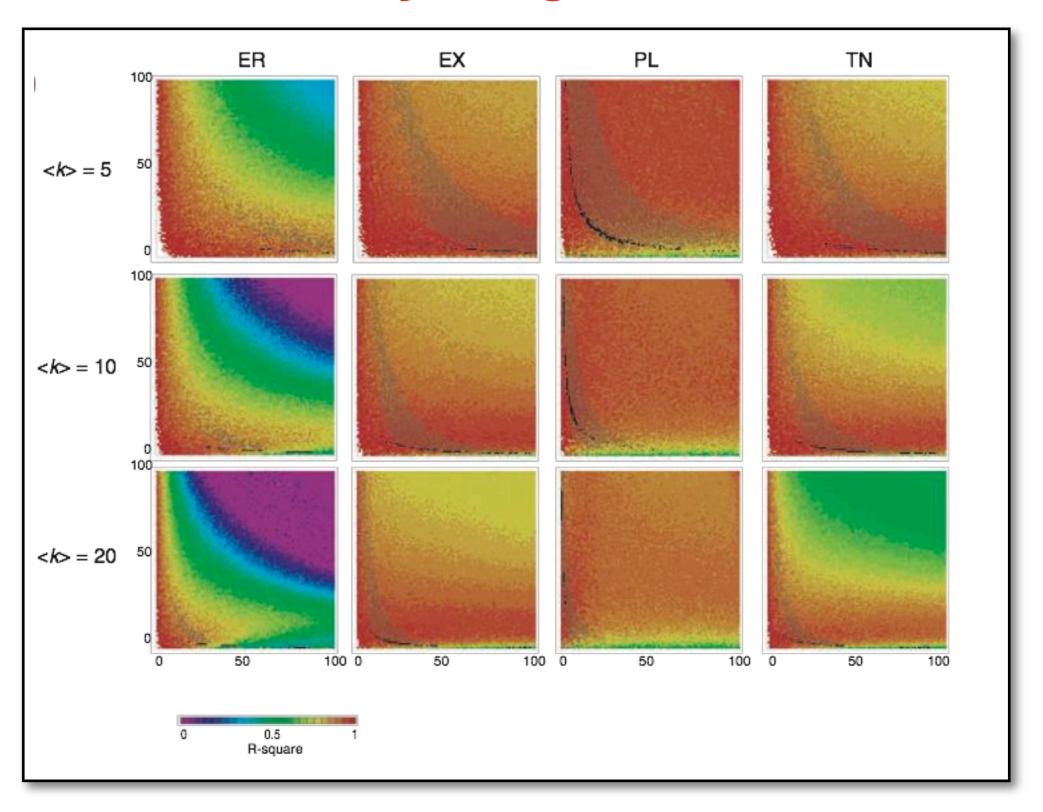


Sparsely Sampled random (ER) Network

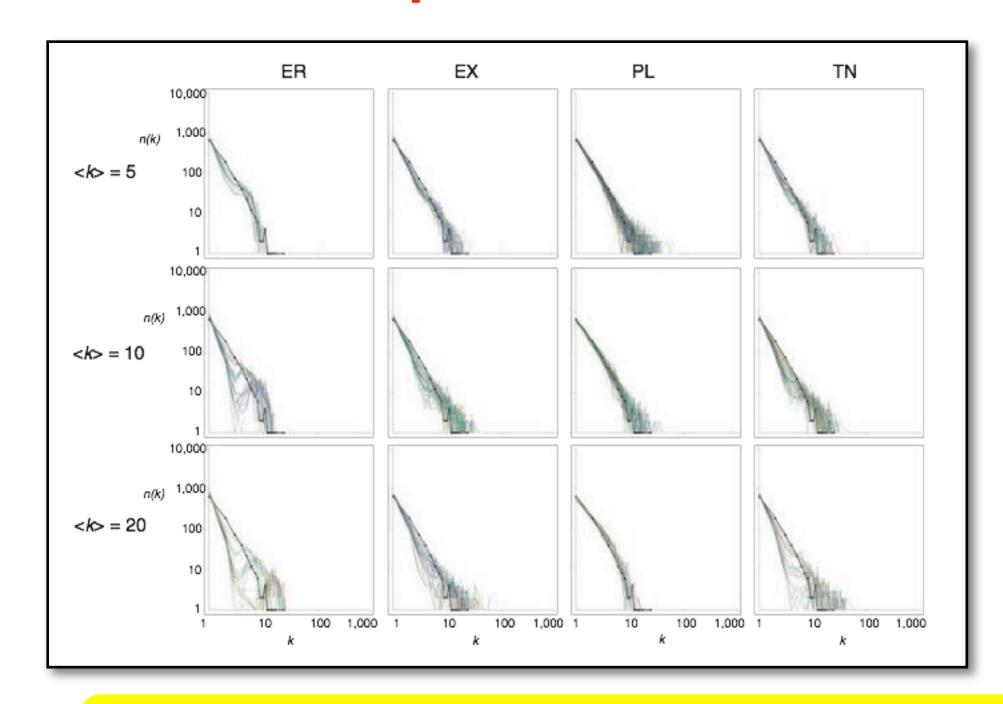


→ for sparse sampling (10-20%), even an ER networks "looks" scale-free (when only P(k) is considered)

Anything Goes



Compare to Uetz et al. Data



Uetz et al. data (solid line) is compared to sampled networks of similar size.

Sampling density affects observed degree distribution

→ true underlying network cannot be identified from available data

Network Growth Mechanisms

Given: an observed PPI network → how did it grow (evolve)?

Inferring network mechanisms: The *Drosophila* melanogaster protein interaction network

Manuel Middendorf[†], Etay Ziv[‡], and Chris H. Wiggins^{§¶}

[†]Department of Physics, [‡]College of Physicians and Surgeons, [§]Department of Applied Physics and Applied Mathematics, and [¶]Center for Computational Biology and Bioinformatics, Columbia University, New York, NY 10027

Communicated by Barry H. Honig. Columbia University. New York. NY. December 20, 2004 (received for review September 7, 2004).

PNAS 102 (2005) 3192

Look at **network motifs** (local connectivity): compare motif distributions from various network prototypes to fly network

Idea: each growth mechanism leads to a typical motif distribution, even if global measures are comparable

The Fly Network

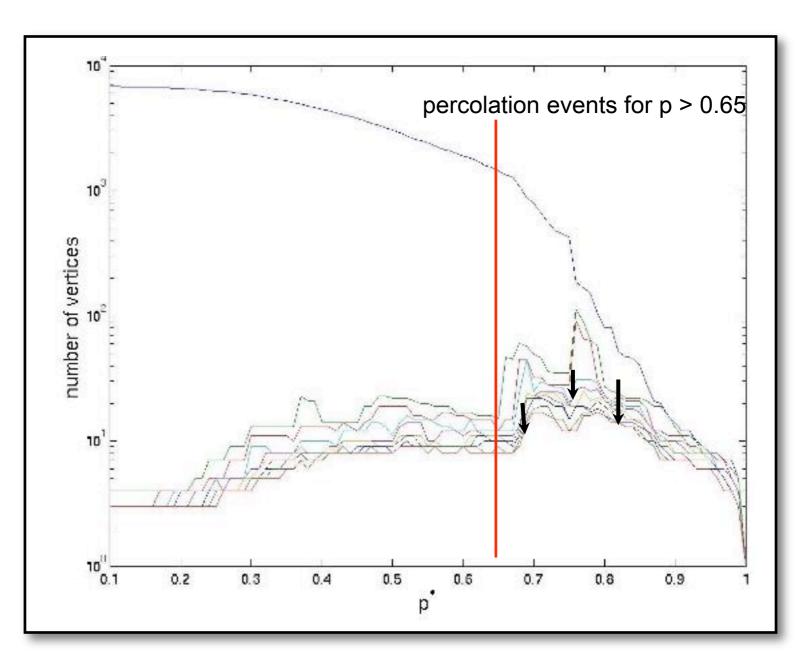
Y2H PPI network for *D. melanogaster* from Giot et al. [Science 302 (2003) 1727]

Confidence score [0, 1] for every observed interaction

- \rightarrow use only data with p > 0.65 (0.5)
- → remove self-interactions and isolated nodes

High confidence network with 3359 (4625) nodes and 2795 (4683) edges

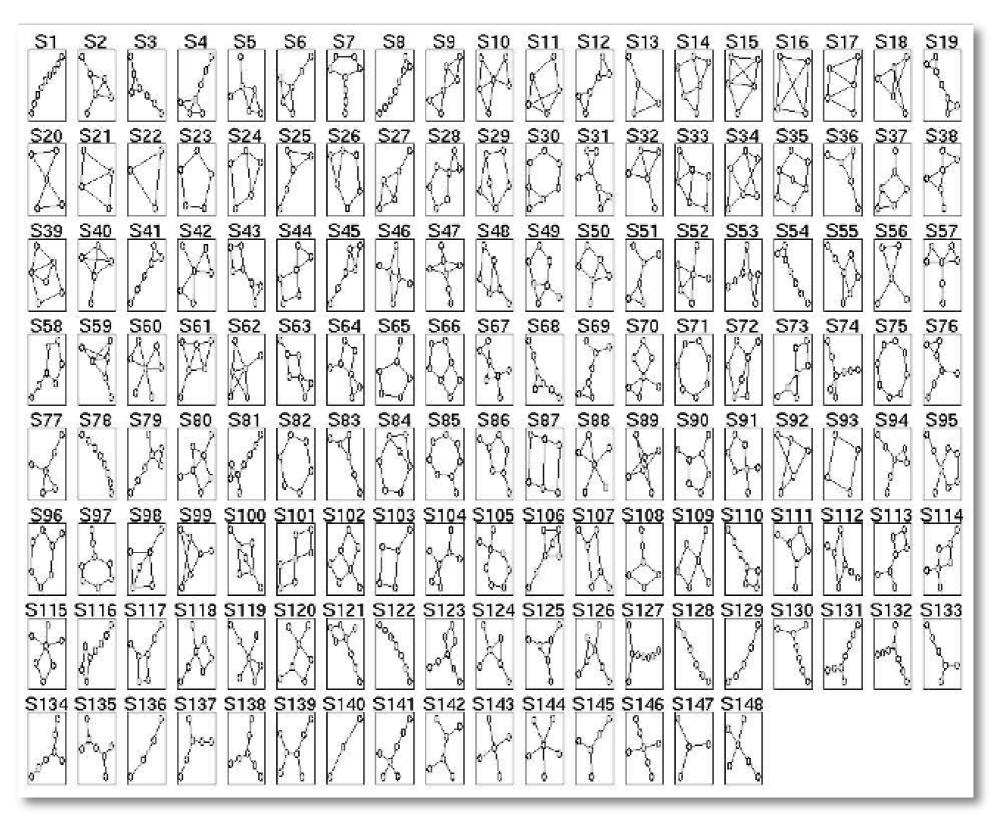
Use prototype networks of same size for training



Size of largest components. At p = 0.65, there is one large component with 1433 nodes and the other 703 components contain at most 15 nodes.

Network Motives

All non-isomorphic subgraphs that can be generated with a walk of length 8



Growth Mechanisms

Generate 1000 networks, each, of the following 7 types (same size as fly network, undefined parameters were scanned)

DMC Duplication-mutation, preserving complementarity

DMR Duplication with random mutations

RDS Random static networks

RDG Random growing network

LPA Linear preferential attachment network (Albert-Barabasi)

AGV Aging vertices network

SMW Small world network

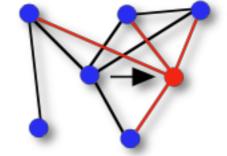
Growth Type 1: DMC

"Duplication – mutation with preserved complementarity"

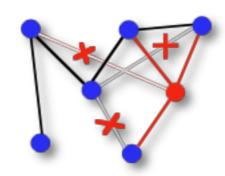
Evolutionary idea: gene **duplication**, followed by a partial **loss** of function of one of the copies, making the other copy essential

Algorithm:

Start from two connected nodes, repeat *N* - 2 times:



- duplicate existing node with all interactions
- for all neighbors: delete with probability q_{del}
 either link from original node or from copy



Growth Type 2: DMR

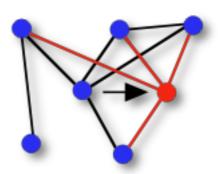
"Duplication with random mutations"

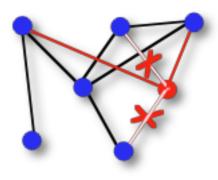
Gene duplication, but no correlation between original and copy (original unaffected by copy)

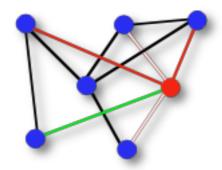
Algorithm:

Start from five-vertex cycle, repeat *N* - 5 times:

- duplicate existing node with all interactions
- for all neighbors: delete with probability q_{del} link from copy
- add new links to non-neighbors with probability q_{new}/n







Growth Types 3–5: RDS, RDG, and LPA

RDS = static random network

Start from N nodes, add L links randomly

RDG = growing random network

Start from small random network, add nodes, then edges between all existing nodes

LPA = linear preferential attachment

Add new nodes similar to Barabási-Albert algorithm, but with preference according to $(k_i + \alpha)$, $\alpha = 0...5$ (BA for $\alpha = 0$)

Growth Types 6-7: AGV and SMW

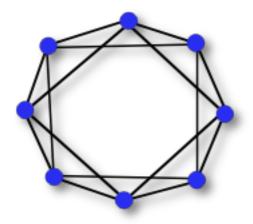
AGV = aging vertices network

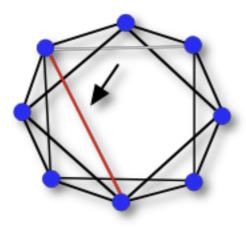
Like growing random network, but preference decreases with age of the node

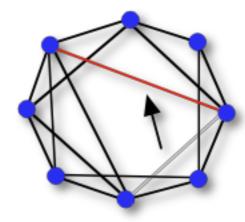
→ citation network: more recent publications are cited more likely

SMW = small world networks (Watts, Strogatz, *Nature* **363** (1998) 202)

Randomly rewire regular ring lattice

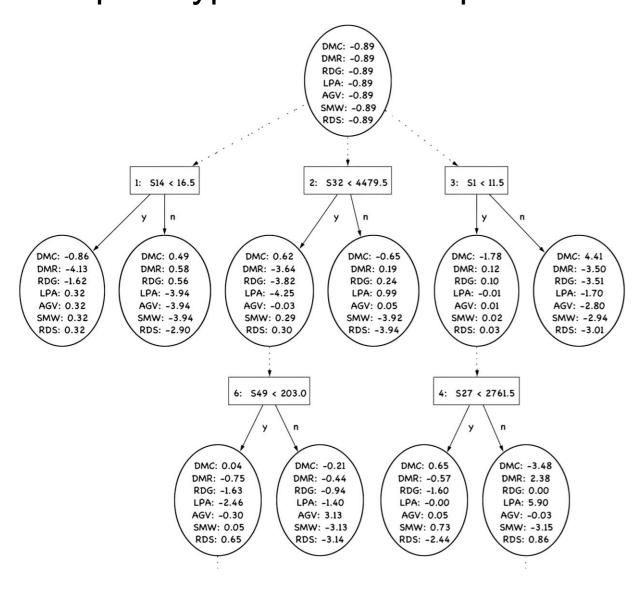






Alternating Decision Tree Classifier

Trained with the motif counts from 1000 networks of each of the 7 types → prototypes are well separated and reliably classified



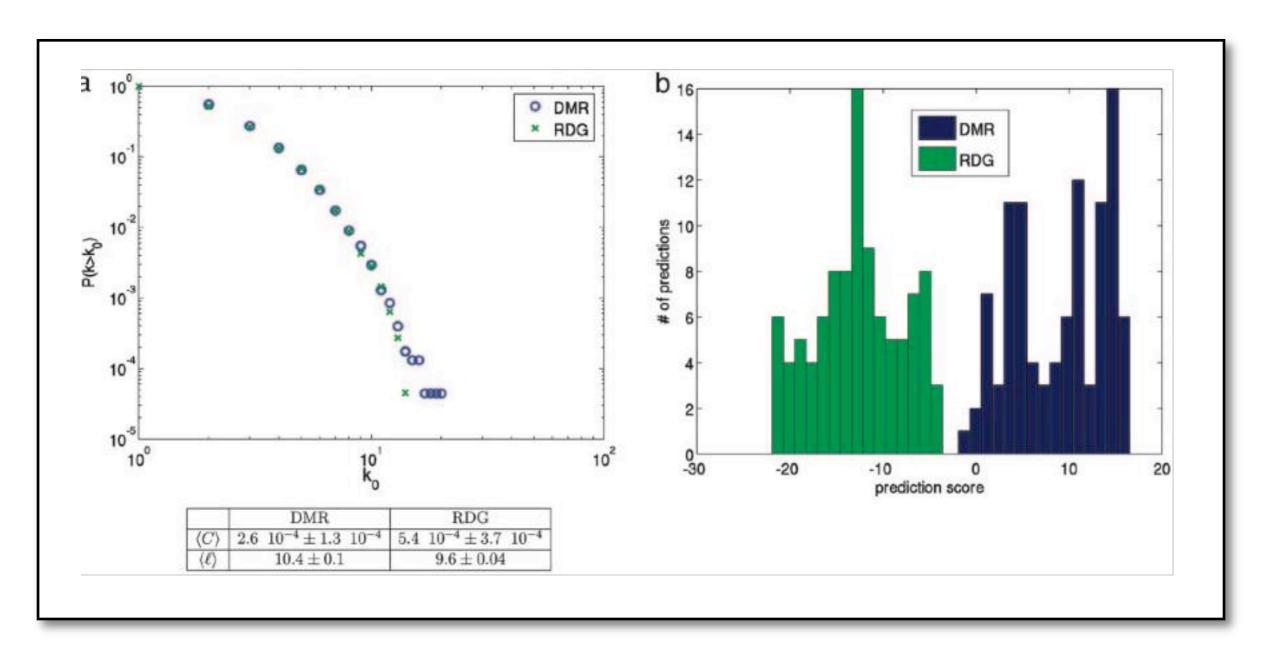
Prediction accuracy for networks similar to fly network with p = 0.5:

Truth	Prediction								
	DMR	DMC	AGV	LPA	SMW	RDS	RDG		
DMR	99.3	0.0	0.0	0.0	0.0	0.1	0.6		
DMC	0.0	99.7	0.0	0.0	0.3	0.0	0.0		
AGV	0.0	0.1	84.7	13.5	1.2	0.5	0.0		
LPA	0.0	0.0	10.3	89.6	0.0	0.0	0.1		
SMW	0.0	0.0	0.6	0.0	99.0	0.4	0.0		
RDS	0.0	0.0	0.2	0.0	8.0	99.0	0.0		
RDG	0.9	0.0	0.0	0.1	0.0	0.0	99.0		

Part of a trained ADT

Decision nodes count occurrence of motifs

Are They Different?



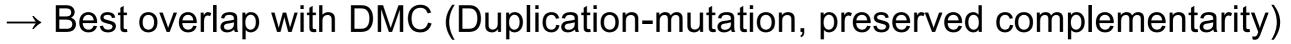
Example DMR vs. RDG: Similar global parameters <C> and <l> (left), but different counts of the network motifs (right)

-> networks can (only) be perfectly separated by motif-based classifier

How Did the Fly Evolve?

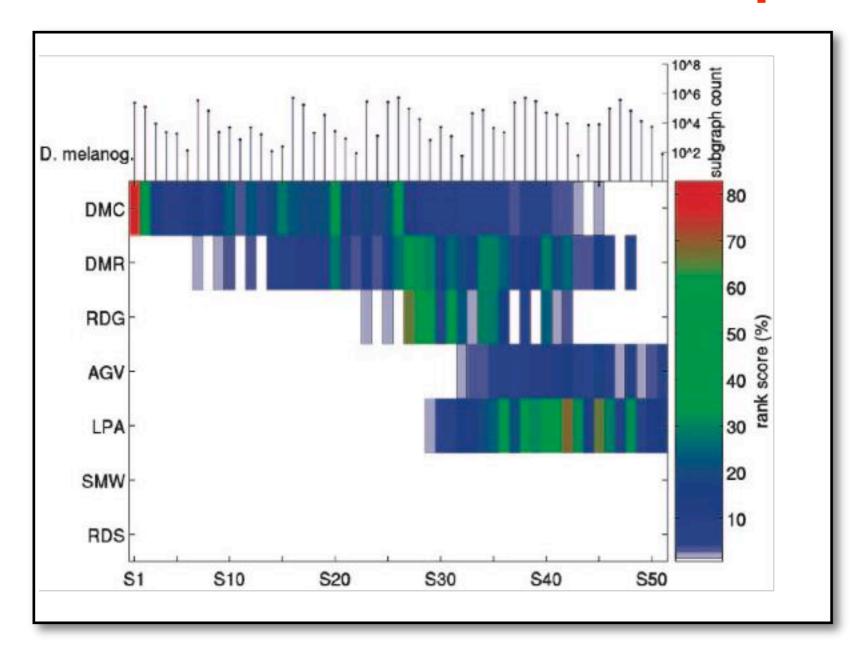
	Eight-step subgraphs $(p* = 0.65)$		se	phs with up to ven edges * = 0.65)	Eight-step subgraphs $(p* = 0.5)$	
Rank	Class	Score	Class	Score	Class	Score
1	DMC	8.2 ± 1.0	DMC	8.6 ± 1.1	DMC	0.8 ± 2.9
2	DMR	-6.8 ± 0.9	DMR	-6.1 ± 1.7	DMR	-2.1 ± 2.0
3	RDG	-9.5 ± 2.3	RDG	-9.3 ± 1.6	AGV	-3.1 ± 2.2
4	AGV	-10.6 ± 4.2	AGV	-11.5 ± 4.1	LPA	-10.1 ± 3.1
5	LPA	-16.5 ± 3.4	LPA	-14.3 ± 3.2	SMW	-20.6 ± 1.9
6	SMW	-18.9 ± 0.7	SMW	-18.3 ± 1.9	RDS	-22.3 ± 1.7
7	RDS	-19.1 ± 2.3	RDS	-19.9 ± 1.5	RDG	-22.5 ± 4.7

Drosophila is consistently (independently of the cut-off in subgraph size) classified as a DMC network, with an especially strong prediction for a confidence threshold of $p^* = 0.65$.



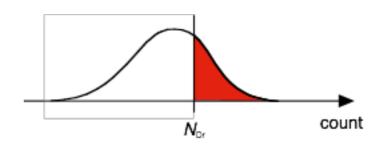
→ Scale-free or random networks are very unlikely

Motif Count Frequencies



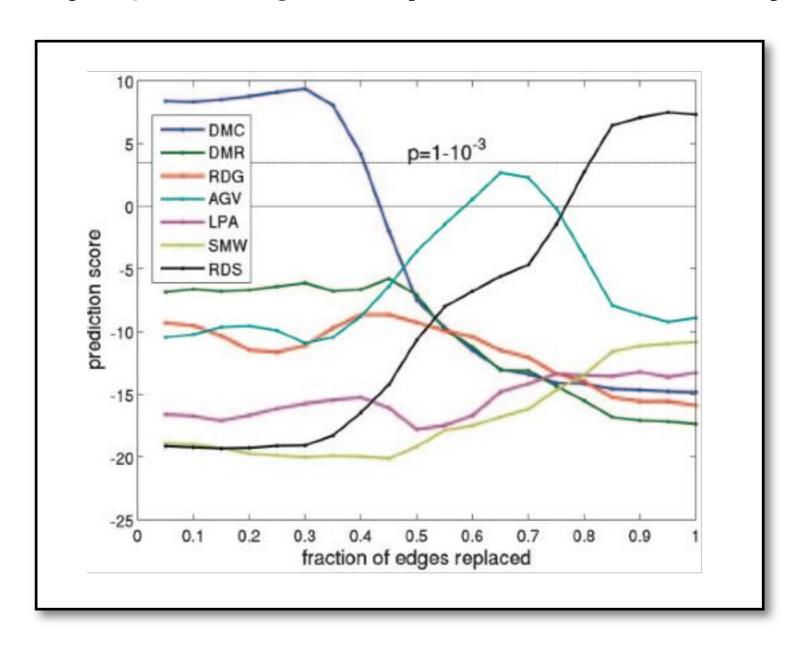
-> DMC and DMR networks contain most subgraphs in similar amount as fly network (top).

rank score: fraction of test networks with a higher count than Drosophila (50% = same count as fly on avg.)



Experimental Errors?

Randomly replace edges in fly network and classify again:



→ Classification unchanged for ≤ 30% incorrect edges, at higher values RDS takes over (as to be expected)

Summary (I)

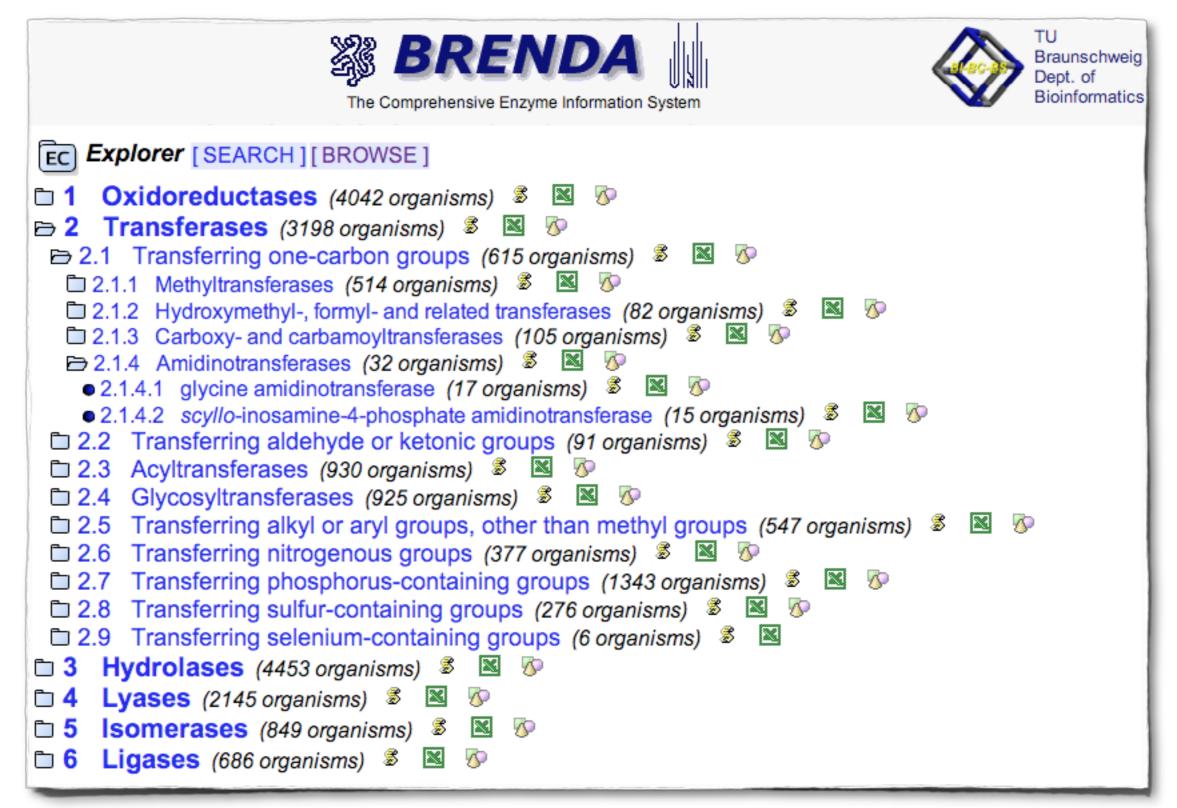
Sampling matters!

 \rightarrow "Scale-free" P(k) obtained by sparse sampling from many network types

Test different **hypotheses** for

- global features
 - → depends on unknown parameters and sampling
 - → no clear statement possible
- local features (motifs)
 - → are better preserved
 - → DMC best among tested prototypes

What Does a Protein Do?



Enzyme Classification scheme (from http://www.brenda-enzymes.org/)

Un-Classified Proteins?

BIOINFORMATICS

Vol. 21 Suppl. 1 2005, pages i302–i310 doi:10.1093/bioinformatics/bti1054



Whole-proteome prediction of protein function via graph-theoretic analysis of interaction maps

Elena Nabieva^{1,2}, Kam Jim², Amit Agarwal¹, Bernard Chazelle¹ and Mona Singh^{1,2,*}

¹Computer Science Department and ²Lewis-Sigler Institute for Integrative Genomics, Princeton University, Princeton, NJ 08544, USA

Received on January 15, 2005; accepted on March 27, 2005

Many unclassified proteins:

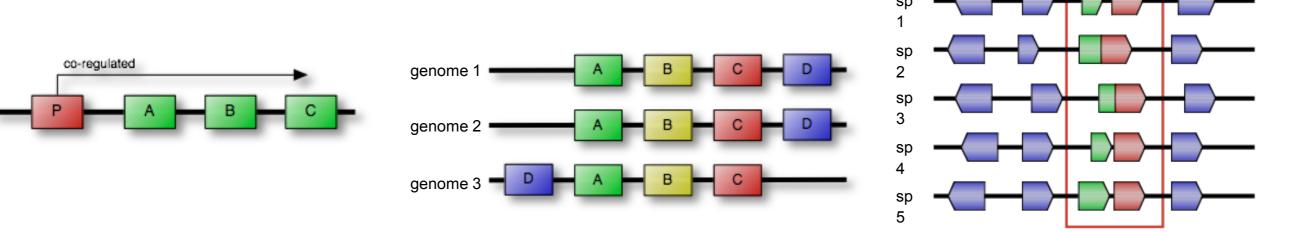
- → estimate: ~1/3 of the yeast proteome not annotated functionally
- → BioGRID: 4495 proteins in the largest cluster of the yeast physical interaction map.

2946 have a MIPS functional annotation

Partition the Graph

Large **PPI networks** were built from:

- HT experiments (Y2H, TAP, synthetic lethality, coexpression, coregulation, ...)
- predictions (gene profiling, gene neighborhood, phylogenetic profiles, ...)
- → proteins that are functionally linked



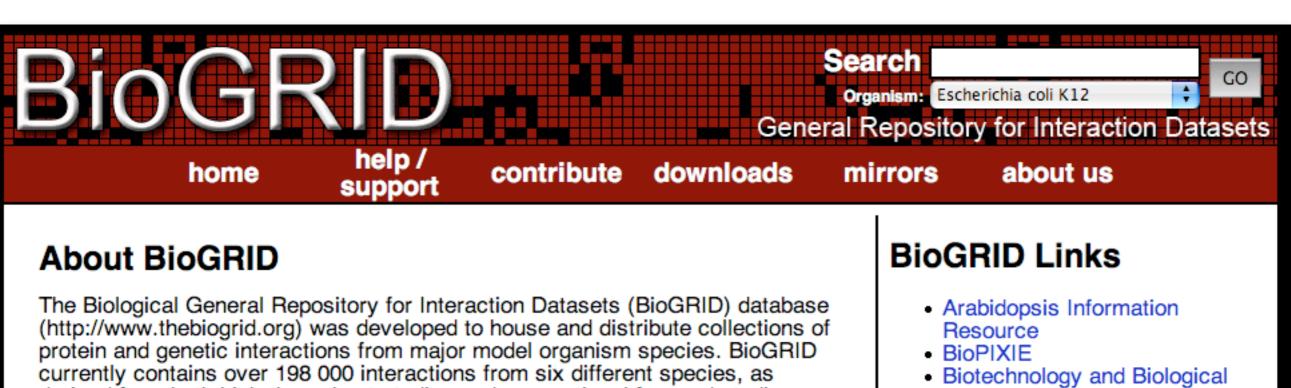
Identify unknown functions from clustering of these networks by, e.g.:

- shared interactions (similar neighborhood → power graphs)
- membership in a community
- similarity of shortest path vectors to all other proteins (= similar path into the rest of the network)

Protein Interactions

Nabieva et al used the *S. cerevisiae* dataset from GRID of 2005 (now BioGRID)

→ 4495 proteins and 12 531 physical interactions in the largest cluster



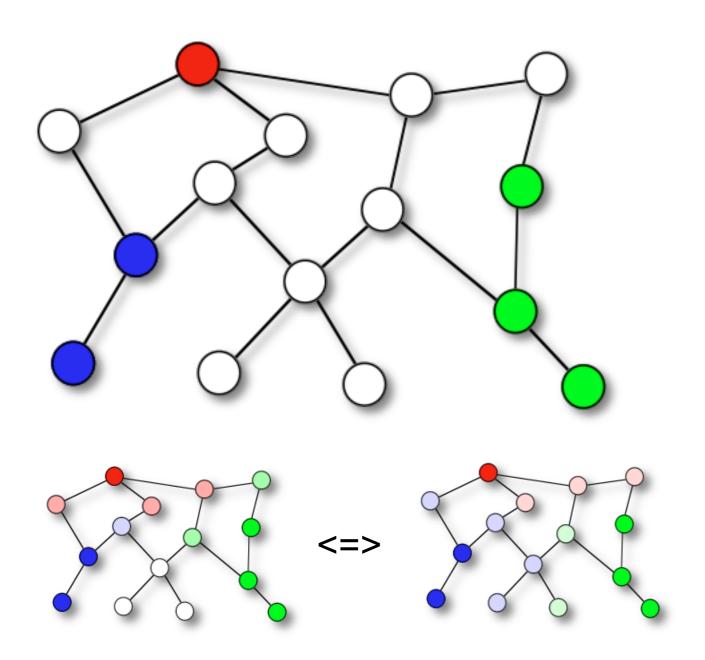
The Biological General Repository for Interaction Datasets (BioGRID) database (http://www.thebiogrid.org) was developed to house and distribute collections of protein and genetic interactions from major model organism species. BioGRID currently contains over 198 000 interactions from six different species, as derived from both high-throughput studies and conventional focused studies. Through comprehensive curation efforts, BioGRID now includes a virtually complete set of interactions reported to date in the primary literature for both the budding yeast Saccharomyces cerevisiae and the fission yeast Schizosaccharomyces pombe. A number of new features have been added to the BioGRID including an improved user interface to display interactions based on different attributes, a mirror site and a dedicated interaction management system to coordinate curation across different locations. The BioGRID provides interaction data with monthly updates to Saccharomyces Genome Database, Flybase and Entrez Gene. Source code for the BioGRID and the linked Osprey network visualization system is now freely available without restriction.

- Biotechnology and Biological Sciences Research Council (BBSRC)
- Canadian Institutes of Health Research (CIHR)
- Cytoscape
- Database of Interacting Proteins
- Entrez-Gene
- Flybase
- Gene DB
- Gene Ontology
- Germ Online

http://www.thebiogrid.org/about.php

Function Annotation

Task: **predict** function (= functional annotation) for a protein from the **available** annotations



Similar:

How to **assign colors** to the white nodes?

Use information on:

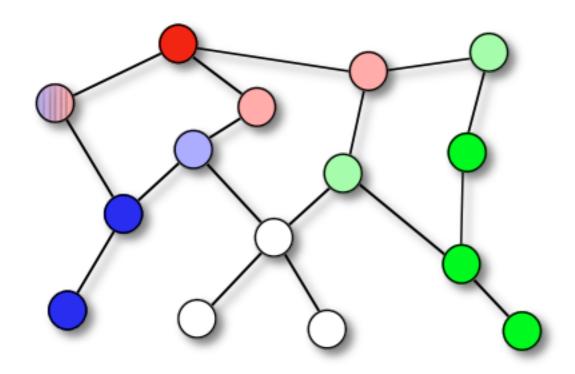
- distance to colored nodes
- local connectivity
- reliability of the links
- ...

Algorithm I: Majority

Schwikowski, Uetz, and Fields, "A network of protein–protein interactions in yeast" *Nat. Biotechnol.* **18** (2000) 1257

Consider all neighbors and sum up how often a certain annotation occurs

- → score for an annotation = count among the direct neighbors
 - → take the 3 most frequent functions



Majority makes only limited use of the local connectivity

→ cannot assign function to next-neighbors

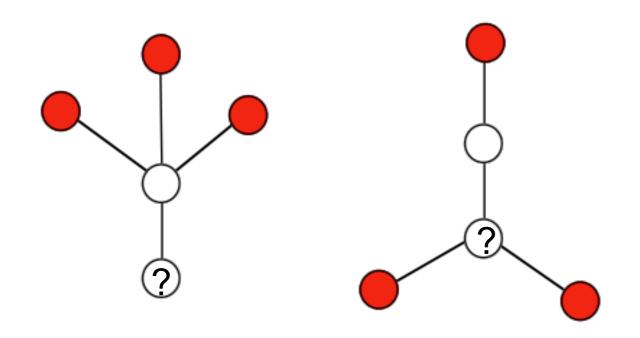
For weighted graphs:

→ weighted sum

Extended Majority: Neighborhood

Hishigaki, Nakai, Ono, Tanigami, and Takagi, "Assessment of prediction accuracy of protein function from protein—protein interaction data", *Yeast* **18** (2001) 523

Look for **overrepresented** functions within a given **radius** of 1, 2, or 3 links \rightarrow use as function score the value of a χ^2 -test



Neighborhood algorithm does not consider local network topology

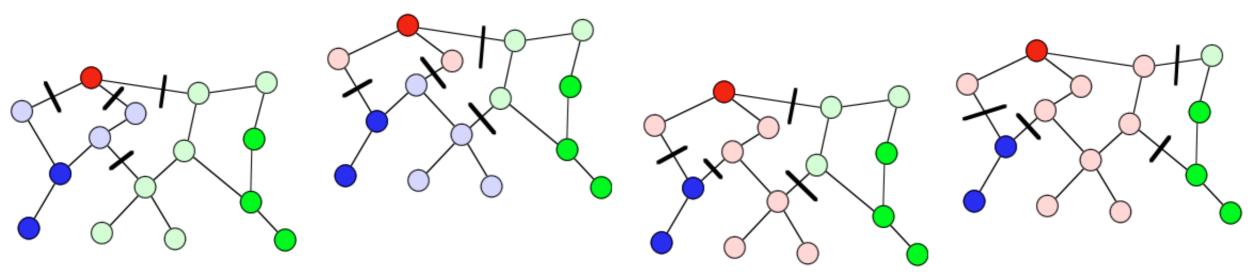
Both examples (left) are treated **identically** with r = 2

Minimize Changes: GenMultiCut

Karaoz, Murali, Letovsky, Zheng, Ding, Cantor, and Kasif, "Whole-genome annotation by using evidence integration in functional-linkage networks" PNAS **101** (2004) 2888

"Annotate proteins so as to **minimize** the number of times that **different** functions are associated with **neighboring** proteins"

→ generalization of the multiway k-cut problem for weighted edges, can be stated as an integer linear program (ILP)



Multiple possible solutions → scores from frequency of annotations

Nabieva et al: FunctionalFlow

Extend the idea of "guilty by association"

- → each annotated protein is a source of "function"-flow
 - → simulate for a few time steps
 - → choose the annotation a with the highest accumulated flow

Each node u has a reservoir $R_t(u)$, each edge a capacity constraint (weight) $w_{u,v}$

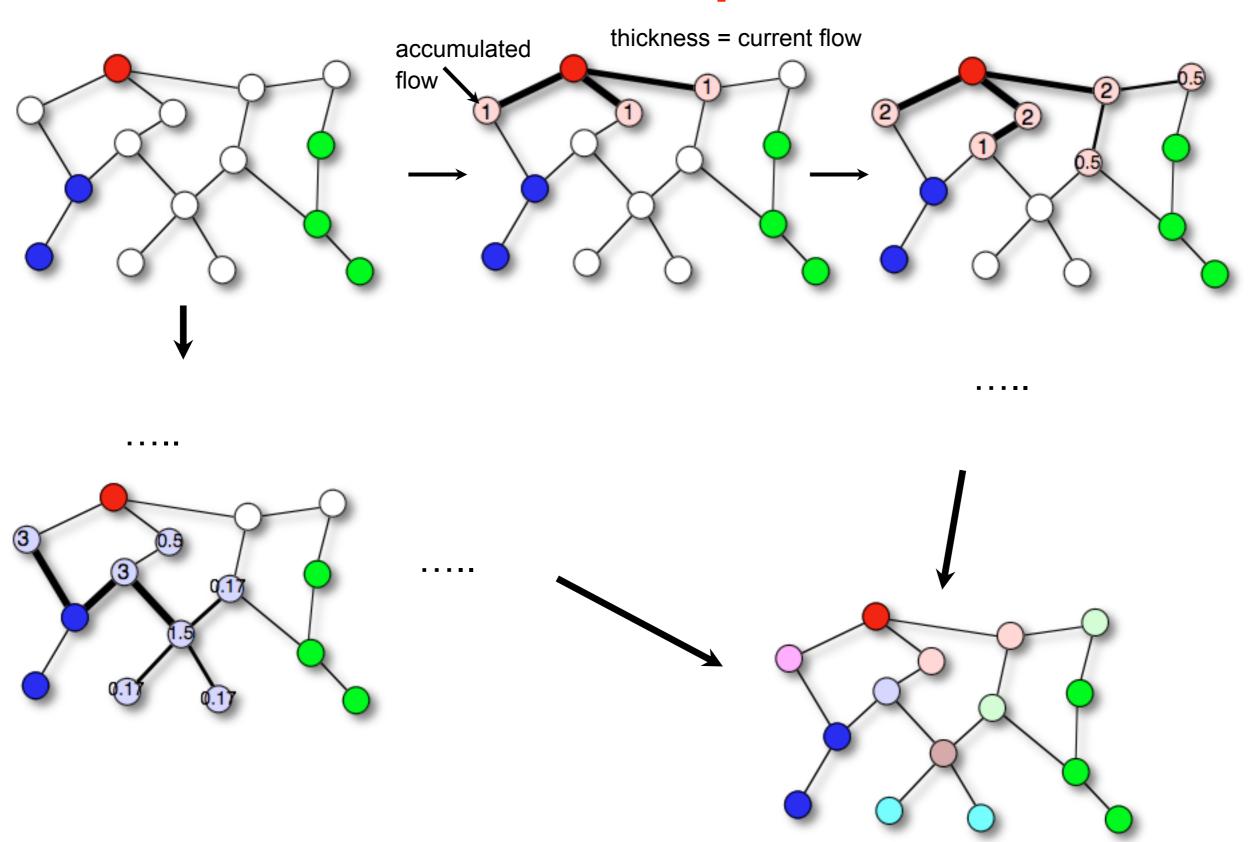
Initially:
$$R_0^a(u) = \begin{cases} \infty, & \text{if } u \text{ is annotated with } a, \\ 0, & \text{otherwise.} \end{cases}$$
 and $g_0^a(u, v) = 0$

Then: downhill flow with capacity constraints

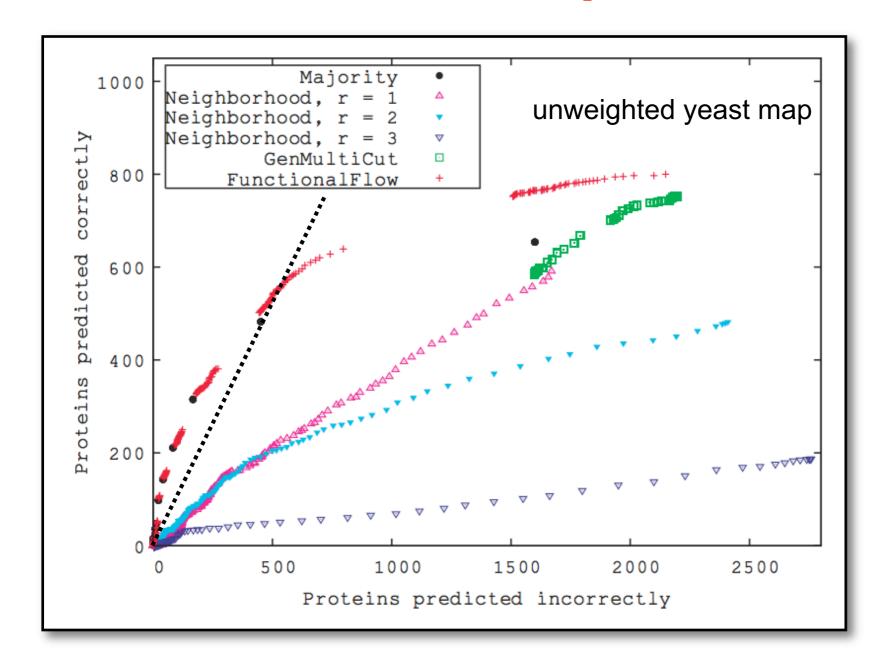
$$g_t^a(u,v) = \begin{cases} 0, & \text{if } R_{t-1}^a(u) < R_{t-1}^a(v) \\ \min\left(w_{u,v}, \frac{w_{u,v}}{\sum_{(u,y) \in E} w_{u,y}}\right), & \text{otherwise.} \end{cases}$$

Score from accumulated in-flow:
$$f_a(u) = \sum_{t=1}^d \sum_{v:(u,v)\in E} g_t^a(v,u)$$

An Example



Comparison



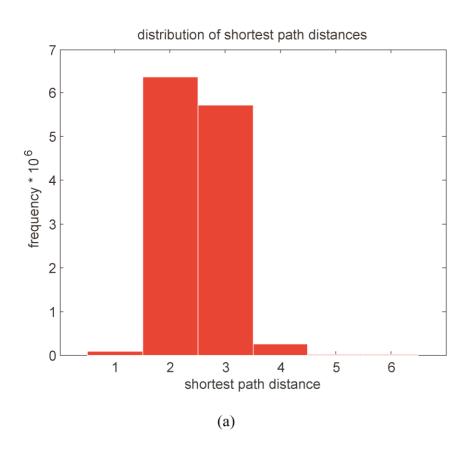
For FunctionalFlow: six propagation steps (diameter of the yeast network ≈ 12)

Change **score threshold** for accepting annotations → ratio **TP/FP**

- → FunctionalFlow performs best in the high-confidence region
- → but many false predictions!!!

Going the Distance for Protein Function Prediction: A New Distance Metric for Protein Interaction Networks

Citation: Cao M, Zhang H, Park J, Daniels NM, Crovella ME, et al. (2013) Going the Distance for Protein Function Prediction: A New Distance Metric for Protein Interaction Networks. PLoS ONE 8(10): e76339. doi:10.1371/journal.pone.0076339



Relying on the ordinary shortest-path distance metric in PPI networks is problematic because PPI networks are "small world" networks.

Most nodes are close to all other nodes.

→ any method that infers similarity based on proximity will find that a large fraction of the network is proximate to any typical node.

Largest connected component of *S. cerevisiae* PPI network (BioGRID) has 4990 nodes and 74,310 edges (physical interactions).

Fig. shows the histogram of shortest-path lengths from this network. Over 95% of all pairs of nodes are either 2 hops or 3 hops apart

What nodes mediate short contacts?

The 2-hop neighborhood of a typical node probably includes around half of **all nodes** in the graph.

One of the **reasons** that paths are typically short in biological networks like the PPI network is due to the **presence of hubs**.

Hubs often represent proteins with *different* functional roles than their neighbors.

Hubs are also more likely to be proteins with multiple, distinct functions.

→ not all short paths provide equally strong evidence of similar function in PPI networks.

DSD Distance Metric

Given some fixed k > 0, we define $He^{\{k\}}(A,B)$ to be the expected number of times that a random walk starting at A and proceeding for k steps, will visit B.

Consider the undirected graph G(V,E) on the vertex set $V = \{v_1, v_2, v_3, ..., v_n\}$ and |V| = n.

$$He(v_i) = (He(v_i, v_1), He(v_i, v_2), ..., He(v_i, v_n))$$

$$DSD(u,v) = ||He(u) - He(v)||_1$$

 $||He(u)-He(v)||_1$ denotes the L_1 norm of the He vectors

The one-norm (also known as the L_1 -norm, ℓ_1 norm, or mean norm) of a vector \vec{v} is denoted $\|\vec{v}\|_1$ and is defined as the sum of the absolute values of its components:

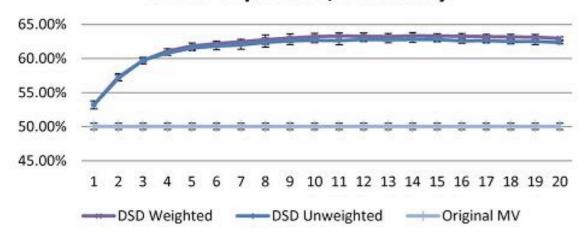
$$\|\vec{v}\|_1 = \sum_{i=1}^n |v_i| \tag{1}$$

for example, given the vector $\vec{v} = (1, -4, 5)$, we calculate the one-norm:

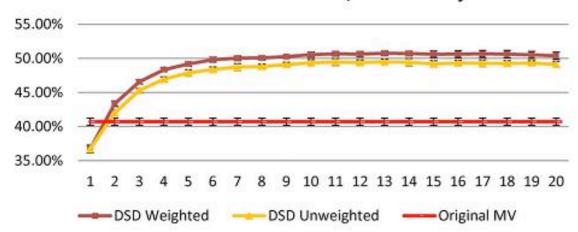
$$||(1, -4, 5)||_1 = |1| + |-4| + |5| = 10$$

DSD clearly improves functional predictions

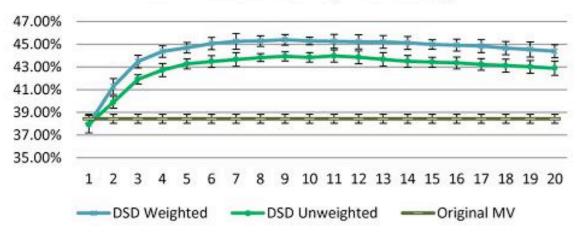
MIPS Top Level, Accuracy



MIPS Second Level, Accuracy



MIPS Third Level, Accuracy



F1 Score on GO term Prediction for S. cerevisiae

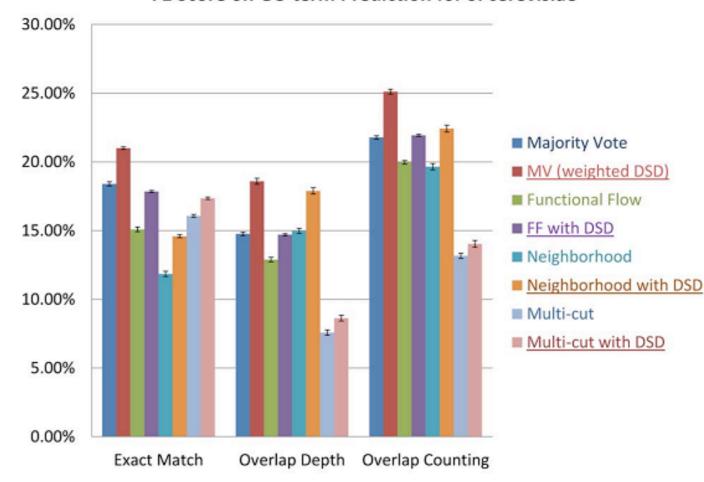
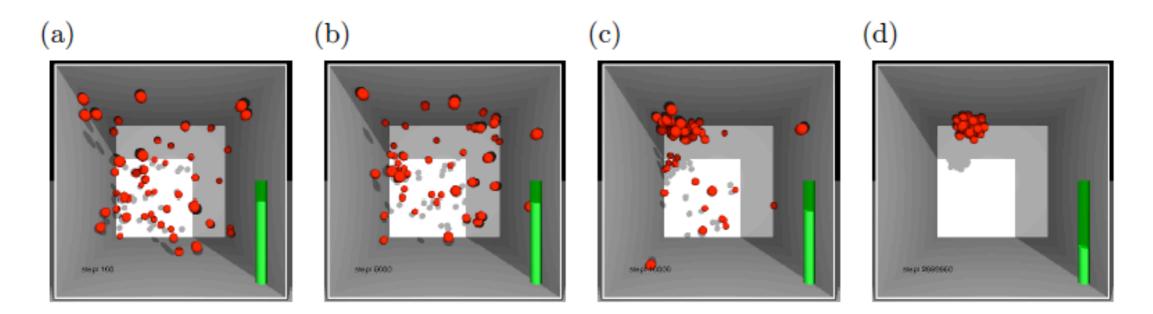


Figure 6. Improvement on F1 Score for DSD using three evaluation methods: exact match, overlap depth and overlap counting, on informative GO terms for the four algorithms for *S. cerevisiae* in 10 runs of 2-fold cross validation.

What you can else do with Interaction graphs?

E.g. efficiently tracking interactions between many particles In dynamics simulations

Strongly attracting particles form large "blob"



How can one analyze the particle connectivity efficiently?

```
For i = 1 to N-1

For j = i to N

For k = j to N

If (i .is bound to. j) then

If (j .is bound to. k) then ....

M.Sc. thesis Florian Lauck (2006)
```

Map simulation to interaction graph

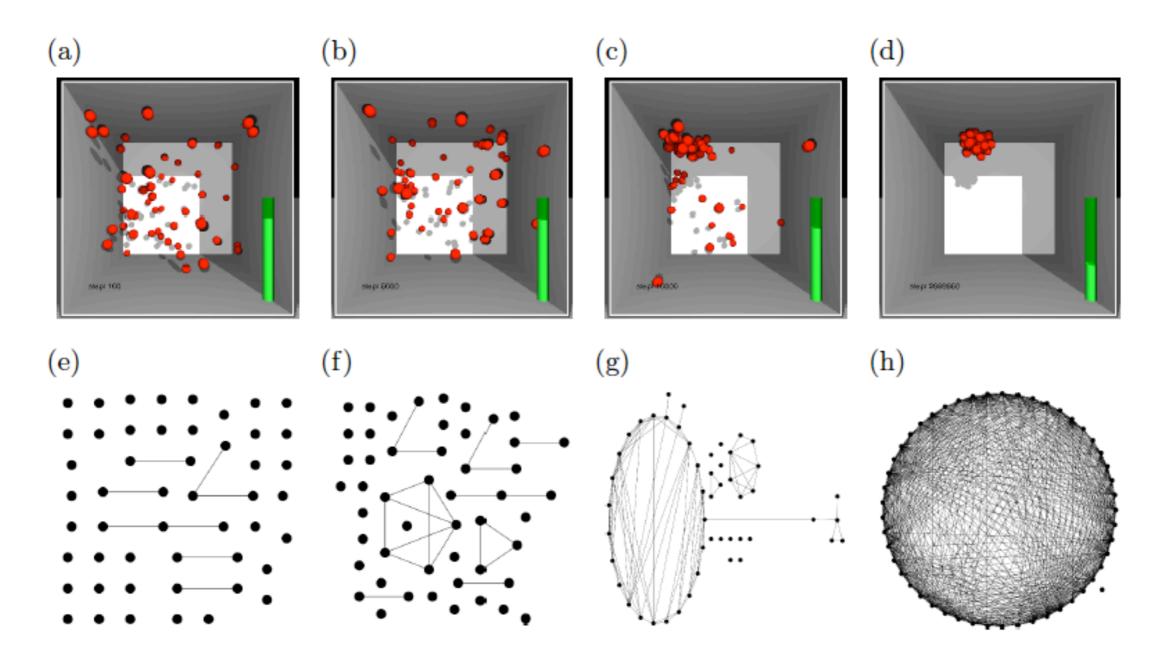
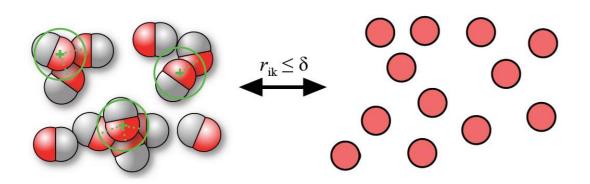


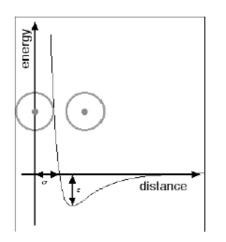
Figure 2.7: Graph and spatial view of a simulation with 50 particles at four different points in time. The green bar denotes the energy of the system.

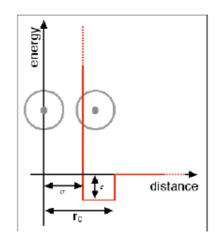
M.Sc. thesis Florian Lauck (2006)

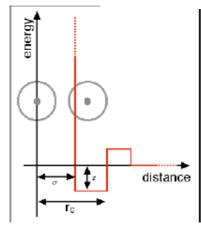
Large number of simultaneous assocications: map simulations to interaction graphs



Simple MC scheme for diffusion + association/ dissociation

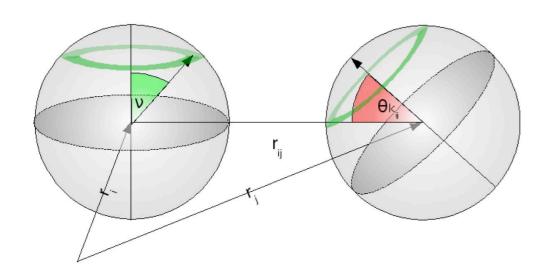






```
function Initialize(N)
   for P \in List of Particles do
      CREATE RANDOM COORDINATES(P)
   CREATE GRAPH(N)
for all Iterations do
   for P \in List of Particles do
      Move and Rotate(P)
      for all P_i \in (\text{List of Particles - P}) do
         d = DISTANCE(P, P_i)
         e_i = \text{POTENTIAL}(d)
         if d \leq r_C then APPEND(List of Interactions, (P, P_i))
         E_{new} += e_i
      a = Transition Probability(E_{new}, E_{old})
      x = RANDOMNUMBER
      if x \le p then
                                                           ▷ accept new state
         Append(List of ALL interactions, List of Interactions)
         E_{old} = E_{new}
      else
                                                           Reset(P) Clear(List of Interactions)
   UPDATE(Graph, List of ALL Interactions)
   Analysis(Graph)
```

Interaction patches define complex geometry

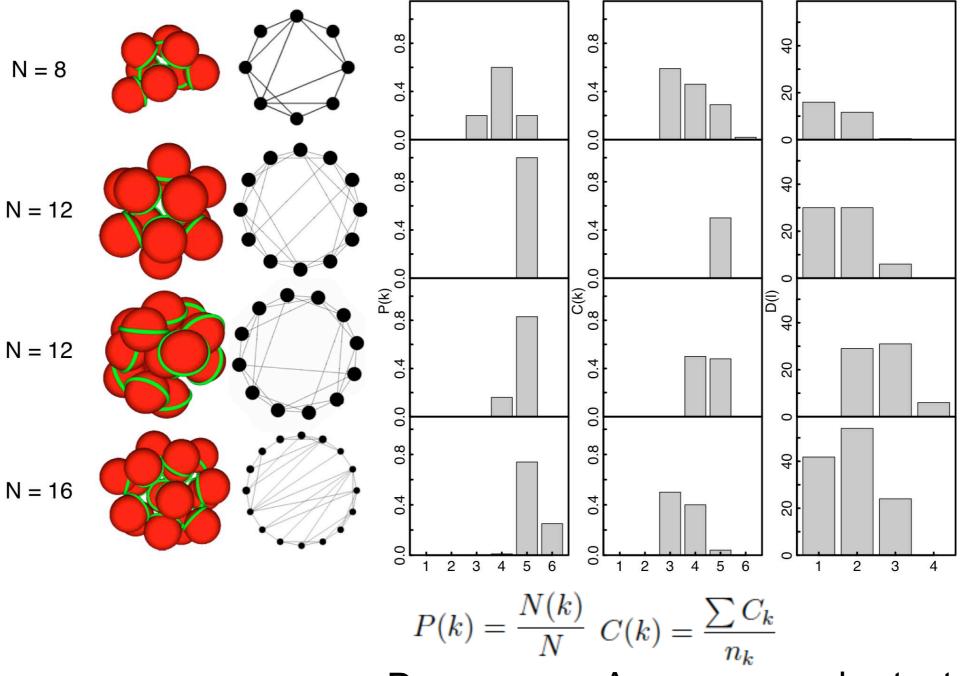


$$G_{ij}(r_{ij}, \theta_{ij}) = \exp\left[\frac{(\theta_{ij} - \nu)}{2\sigma_{PW}^2}\right]$$

$$V_{total} = V(r_{ij}) \times G_{ij}(r_{ij}, \theta_{ij}) \times G_{ji}(r_{ij}, \theta_{ji})$$

Lauck et al., *JCTC 5, 641* (2009)

Assembly of icosahedral complexes

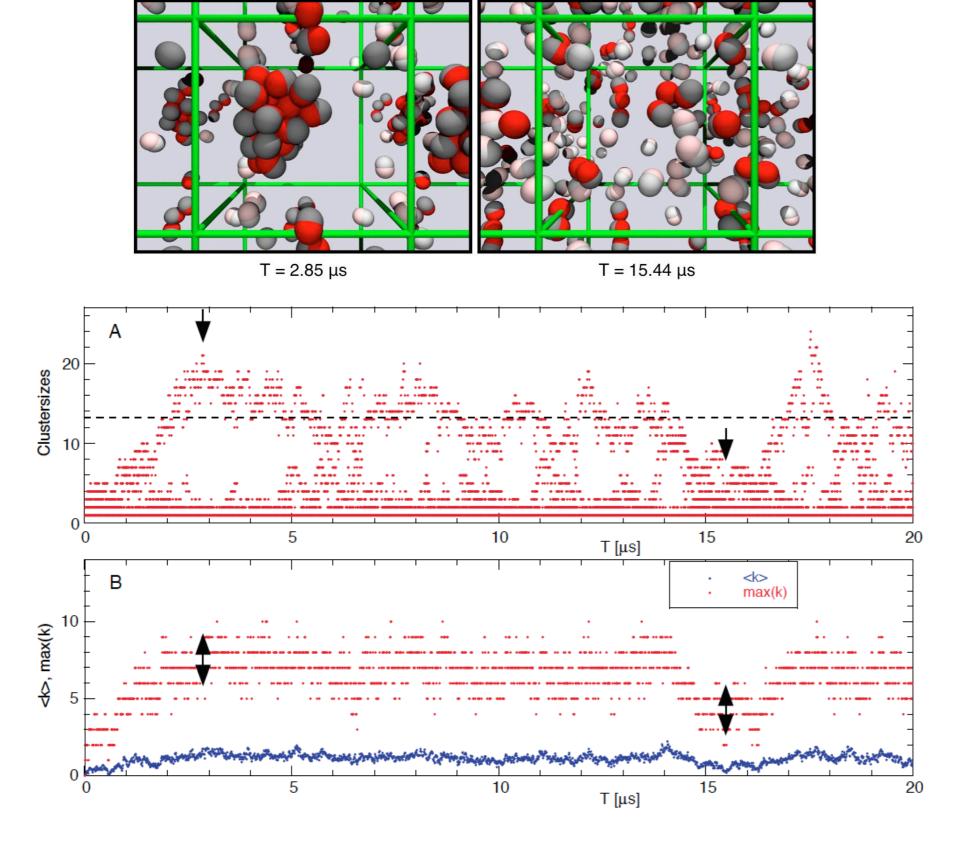


Lauck et al., *JCTC 5, 641* (2009)

Degree distribution

Average Cluster coefficient shortest pathways between nodes

Dynamical view at particle agglomeration



Two snapshots

T = 2.85 μs most of the particles are part of a large cluster,

T = 15.44 µs largest cluster has 3 particles.

Geyer, *BMC Biophysics* (2011)

Summary: Static PPI-Networks

"Proteins are modular machines" <=> How are they related to each other?

- 1) **Understand** "Networks" prototypes (ER, SF, ...) and their properties (*P(k), C(k),* clustering, ...)
- 2) Get the **data** experimental and theoretical techniques (Y2H, TAP, co-regulation, ...), quality control and data integration (Bayes)
- 3) **Analyze** the data compare P(k), C(k), clusters, ... to prototypes \rightarrow highly modular, clustered with sparse sampling \rightarrow PPI networks are not scale-free
- 4) **Predict** missing information network structure combined from multiple sources → functional annotation

Next step: environmental changes, cell cycle

→ changes (dynamics) in the PPI network – how and why?