

# VII

# SBML und Modell- Erstellung

24. Januar 2013

# Übersicht

Austausch und Archivierung von biochemischen Modellen  
=> SBML

Diffusion plus Reaktionen  
=> Virtual Cell

Komplexität der Modelle  
=> BioNetGen

# Systems Biology Markup Language



XML-Dialekt für Speicherung und Austausch  
biochemischer Modelle  
=> Archivierung  
=> Transfer von Modellen in andere Softwaretools

## Acknowledgements

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The development of SBML from its inception through 2003 was principally funded by the [Japan Science and Technology Agency](#) under the [ERATO Kitano Symbiotic Systems Project](#).

Additional support has in the past been provided by the following organizations and agencies: the [Systems Biology Institute](#) (Japan), the [University of Hertfordshire](#) (UK), the [Molecular Sciences Institute](#) (USA), the [National Human Genome Research Institute](#) (USA), the [International Joint Research Program of NEDO](#) (Japan), the [ERATO-SORST](#) Program of the Japan Science and Technology Agency (Japan), the [Ministry of Agriculture](#) (Japan), the [Ministry of Education, Culture, Sports, Science and Technology](#) (Japan), the [BBSRC e-Science Initiative](#) (UK), the [DARPA IPTO Bio-Computation Program](#) (USA), the Army Research Office's [Institute for Collaborative Biotechnologies](#) (USA), and the Air Force Office of Scientific Research (USA).

[von http://sbml.org/Acknowledgments](http://sbml.org/Acknowledgments)

# SBML <= XML

XML = eXtensible Markup Language

- hierarchische Baumstruktur:  
=> Schachtelung von <Object> ... </Object> oder <Objekt [Parameter...]/>
- genau ein Wurzelobjekt: <sbml...>

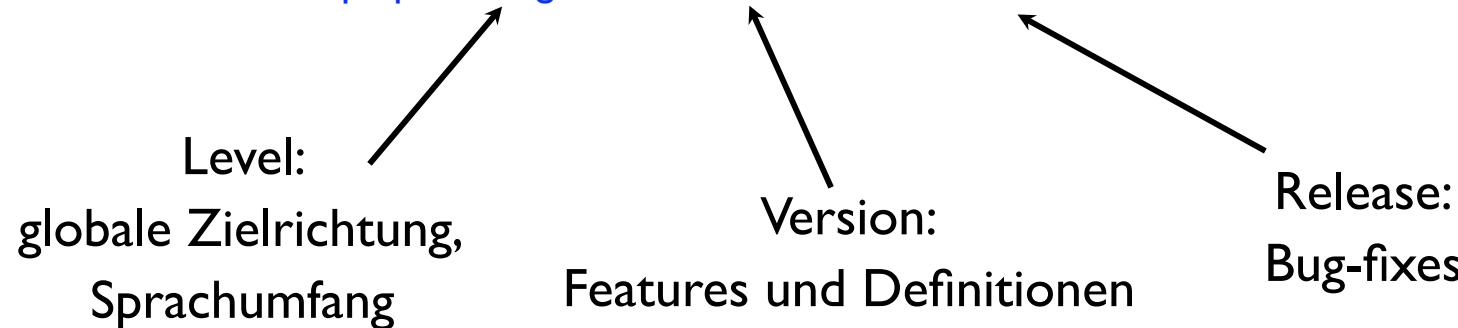
Aktuelle Dialekte: [siehe http://sbml.org/Documents/Specifications](http://sbml.org/Documents/Specifications)

SBML Level 1, Version 2

<http://www.sbml.org/specifications/sbml-level-1/version-2/sbml-level-1-v2.pdf>

SBML Level 2, Version 4, Release 1

<http://precedings.nature.com/documents/2715/version/1>



# Was ist enthalten?

beginning of model definition  
list of function definitions (optional)  
list of unit definitions (optional)  
list of compartment types (optional)  
list of species types (optional)  
list of compartments (optional)  
list of species (optional)  
list of parameters (optional)  
list of initial assignments (optional)  
list of rules (optional)  
list of constraints (optional)  
list of reactions (optional)  
list of events (optional)  
end of model definition

# Ein Beispiel



```

<?xml version="1.0" encoding="UTF-8"?>
<sbml level="2" version="3" xmlns="http://www.sbml.org/sbml/level2/version3">
  <model name="EnzymaticReaction">
    <listOfUnitDefinitions>
      <unitDefinition id="per_second">
        <listOfUnits>
          <unit kind="second" exponent="-1"/>
        </listOfUnits>
      </unitDefinition>
      <unitDefinition id="litre_per_mole_per_second">
        <listOfUnits>
          <unit kind="mole" exponent="-1"/>
          <unit kind="litre" exponent="1"/>
          <unit kind="second" exponent="-1"/>
        </listOfUnits>
      </unitDefinition>
    </listOfUnitDefinitions>
    <listOfCompartments>
      <compartment id="cytosol" size="1e-14"/>
    </listOfCompartments>
    <listOfSpecies>
      <species compartment="cytosol" id="ES" initialAmount="0" name="ES"/>
      <species compartment="cytosol" id="P" initialAmount="0" name="P"/>
      <species compartment="cytosol" id="S" initialAmount="1e-20" name="S"/>
      <species compartment="cytosol" id="E" initialAmount="5e-21" name="E"/>
    </listOfSpecies>
    <listOfReactions>
      <reaction id="veq">
        <listOfReactants>
          <speciesReference species="E"/>
          <speciesReference species="S"/>
        </listOfReactants>
        <listOfProducts>
          <speciesReference species="ES"/>
        </listOfProducts>
        <kineticLaw>
          <math xmlns="http://www.w3.org/1998/Math/MathML">
            <apply>
              <times/>
            </apply>
          </math>
        </kineticLaw>
      </reaction>
    </listOfReactions>
  </model>
</sbml>

```

```

<ci>cytosol</ci>
<apply>
  <minus/>
  <apply>
    <times/>
    <ci>kon</ci>
    <ci>E</ci>
    <ci>S</ci>
  </apply>
  <apply>
    <times/>
    <ci>koff</ci>
    <ci>ES</ci>
  </apply>
</apply>
</math>
<listOfParameters>
  <parameter id="kon" value="1000000" units="litre_per_mole_per_second"/>
  <parameter id="koff" value="0.2" units="per_second"/>
</listOfParameters>
</kineticLaw>
</reaction>
<reaction id="vcat" reversible="false">
  <listOfReactants>
    <speciesReference species="ES"/>
  </listOfReactants>
  <listOfProducts>
    <speciesReference species="E"/>
    <speciesReference species="P"/>
  </listOfProducts>
  <kineticLaw>
    <math xmlns="http://www.w3.org/1998/Math/MathML">
      <apply>
        <times/>
        <ci>cytosol</ci>
        <ci>kcat</ci>
        <ci>ES</ci>
      </apply>
    </math>
    <listOfParameters>
      <parameter id="kcat" value="0.1" units="per_second"/>
    </listOfParameters>
  </kineticLaw>
</reaction>
</listOfReactions>
</model>
</sbml>

```

# Nochmal:



```
<?xml version="1.0" encoding="UTF-8"?>
<sbml level="2" version="3" xmlns="http://www.sbml.org/sbml/level2/version3">
  <model name="EnzymaticReaction">
    <listOfUnitDefinitions>
      :
    </listOfUnitDefinitions>
    <listOfCompartments>
      <compartment id="cytosol" size="1e-14"/>
    </listOfCompartments>
    <listOfSpecies>
      <species compartment="cytosol" id="ES" initialAmount="0" name="ES"/>
      <species compartment="cytosol" id="P" initialAmount="0" name="P"/>
      <species compartment="cytosol" id="S" initialAmount="1e-20" name="S"/>
      <species compartment="cytosol" id="E" initialAmount="5e-21" name="E"/>
    </listOfSpecies>
    <listOfReactions>
      :
    </listOfReactions>
  </model>
</sbml>
```

# Details: Einheiten

```
<listOfUnitDefinitions>
  <unitDefinition id="per_second">
    <listOfUnits>
      <unit kind="second" exponent="-1"/>
    </listOfUnits>
  </unitDefinition>
  <unitDefinition id="litre_per_mole_per_second">
    <listOfUnits>
      <unit kind="mole" exponent="-1"/>
      <unit kind="litre" exponent="1"/>
      <unit kind="second" exponent="-1"/>
    </listOfUnits>
  </unitDefinition>
</listOfUnitDefinitions>
```

per\_seconds :=  $s^{-1}$

$\frac{\text{litre}}{\text{mol s}}$

Screenshot of the SBML Software Matrix page from SBML.org.

The page title is "SBML Software Guide/SBML Software Matrix – SBML.org".

The URL in the address bar is "http://sbml.org/SBML\_Software\_Guide/SBML\_Software\_Matrix".

The page content is titled "SBML Software Matrix". It states: "This matrix provides an at-a-glance summary of software known to us to provide some degree of support for reading, writing, or otherwise working with SBML. The columns' meanings are explained below. For a list of longer descriptions grouped into themes, please see our [SBML Software Summary](#) page."

The table has the following structure:

- Rows:** List of software tools: Cellware, CL-SBML, CLEML, COBRA, ConsensusPathDB, COPASI, Cyto-Sim, Cytoscape, DBSolve, Dizzy, E-CELL, ecell3D, EPE, ESS, ....
- Columns:**
  - Capabilities: Creation, Simulation, Analysis, Database, Utility
  - Frameworks: ODE, DAE, PDE, Stochastic, Events, Logical, Other
  - API: LISP, MATLAB, C++, Java, Python, Java, Java
  - Dep.: L, W, M
  - Platforms: LISP, MATLAB, L, W, M, S
  - SBML: Import, Export
  - Available: Open source, Academic use, Commercial use

	Creation	Simulation	Analysis	Database	Utility	ODE	DAE	PDE	Stochastic	Events	Logical	Other	API	Dep.	Platforms	SBML	Available	
Cellware	*	*				*							LISP	L, W, M	*	*	F \$	
CL-SBML						*							LISP	L	*	*	F F	
CLEML														L, W	*	*	F F	
COBRA		*	*	*	*									MATLAB	L, W, M	*	*	F F
ConsensusPathDB				*											S	*	*	F F
COPASI	*	*	*	*	*	*	*	*					C++, Java, Python		L, W, M	*	*	F \$
Cyto-Sim		*		*				*							L, W, M			F F
Cytoscape	*			*									Java		L, W, M	*		F F
DBSolve	*	*	*	*	*											*	*	F F
Dizzy		*		*				*							L, W, M	*	*	F F
E-CELL	*	*				*									L, W	*	*	F F
eCell3D				*												*		F F
EPE	*		*	*									Java		L, W, M	*		F F
ESS		*													BSP		*	F F
....																		

# Import nach Copasi

The screenshot shows the COPASI 4.5 (Build 30) application window titled "enzymatic - COPASI 4.5 (Build 30) /Users/.../V11/enzymatic.cps". The left sidebar contains a tree view of the model structure:

- Copasi
- Model
  - Biochemical
  - Compartments
    - cytosol
  - Species
    - E
    - ES
    - P
    - S
  - Reactions
    - vcat
    - veq**
  - Global Quantities
  - Parameter Overview
- Mathematical Diagrams
- Tasks
- Output
- Functions

The main panel displays the reaction setup for "veq".

**Reaction Tab:**

- Name: `veq`
- Chemical Equation:  $E + S \rightleftharpoons ES$
- Reversible  Multi Compartment
- Rate Law: Mass action (reversible)
- Flux (mol/s): 0

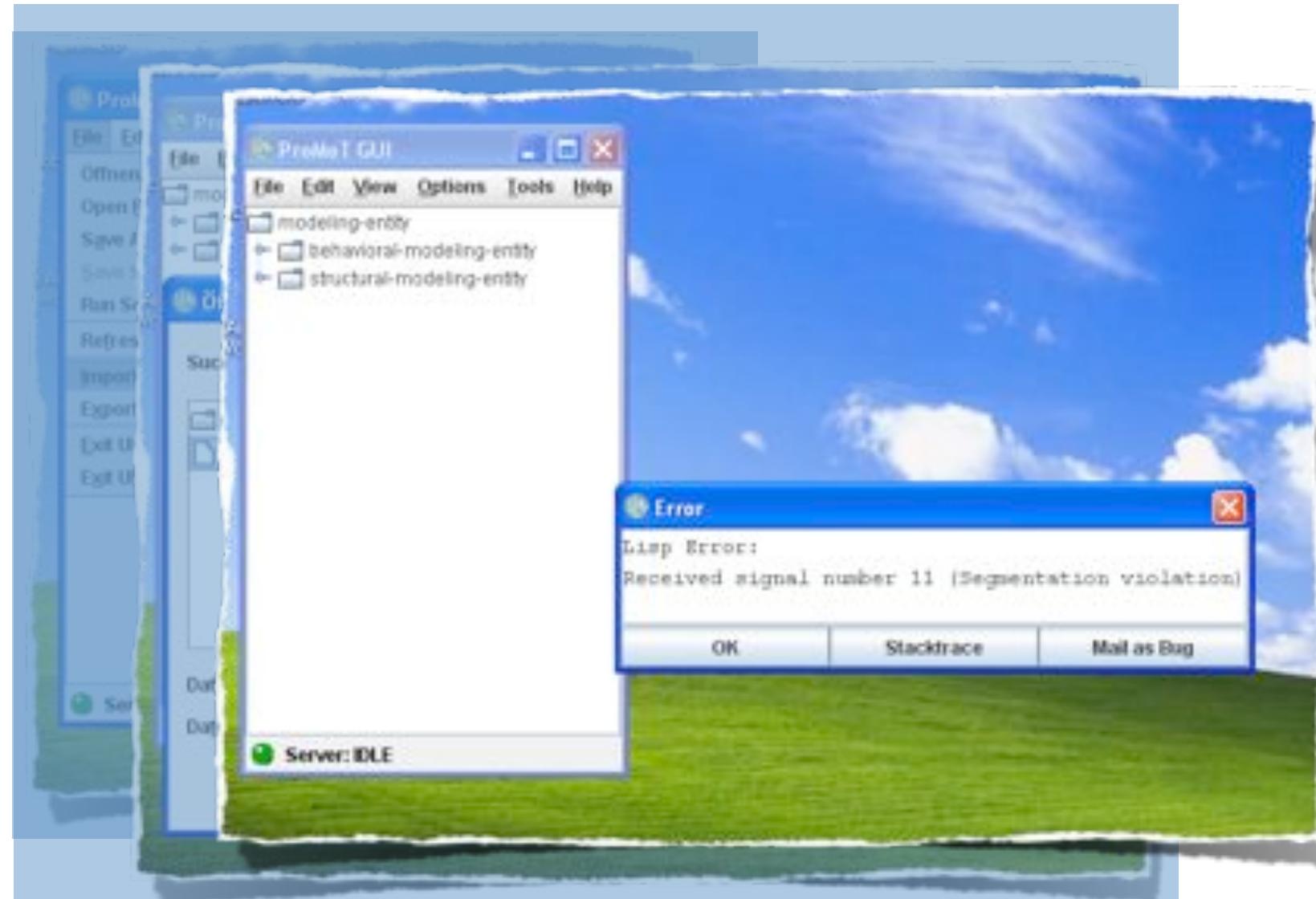
**Symbol Definition Table:**

Description	Name	Value	Unit
Parameter	k1	<input type="checkbox"/> global	$1e+06$ $l/(mol*s)$
Substrate	substrate		mol/l
	E		
	S		
Parameter	k2	<input type="checkbox"/> global	0.2 $l/s$

**Buttons at the bottom:**

- Commit, Revert, New, Delete
- Commit, Revert, Clear, Delete/Undelete, New

# Interoperabilität?



# Details: eine Reaktion

```
<listOfReactions>
  :
<reaction id="vcat" reversible="false">
  <listOfReactants>
    <speciesReference species="ES"/>
  </listOfReactants>
  <listOfProducts>
    <speciesReference species="E"/>
    <speciesReference species="P"/>
  </listOfProducts>
  <kineticLaw>
    <math xmlns="http://www.w3.org/1998/Math/MathML">
      <apply>
        <times/>
        <ci>cytosol</ci>
        <ci>kcat</ci>
        <ci>ES</ci>
      </apply>
    </math>
    <listOfParameters>
      <parameter id="kcat" value="0.1" units="per_second"/>
    </listOfParameters>
  </kineticLaw>
</reaction>
</listOfReactions>
```



$$\Rightarrow \frac{dN}{dt} = V_{cytosol} k_{cat} [ES]$$

lokaler Parameter!

# SBML lesbar machen



**convert**

SBML file:

**Report options**

MIRIAM annotations:  Check SBML consistency:  Include predefined unit declarations:

**Layout options**

Convert to:  Set name in equations:  Landscape:   
Font size:  Reaction participants in one table:  Set identifiers in typewriter font:   
Paper size:  Create a title page:

<http://webservices.cs.uni-tuebingen.de/>

Dräger A, Planatscher H, Wouamba DM, Schröder A, Hucka M, Endler L, Golebiewski M, Müller W, and Zell A: "SBML2LaTeX: Conversion of SBML files into human-readable reports", Bioinformatics 2009

# Drei Minuten später:

The screenshot shows a web interface for converting SBML files. On the left, there's a yellow sidebar with a 'convert' button and a message: 'Please download your result here:' followed by a link '07ff0064-6af4-4eb5-bea1-906da1fbc86-request.pdf'. Below this is a 'Submit another file' button. The main content area is titled 'SBML Model Report' and features the model name 'Model name: "EnzymaticReaction"' in blue. It includes the 'SBML2LATEX' logo and the date 'June 30, 2009'. The report is divided into sections: '1 General Overview', '2 Mathematical Description', '3 Parameters', '4 Species', '5 Reactions', '6 Events', '7 Rules', '8 Constraints', '9 Function Definitions', '10 Unit Definitions', and '11 Initial Assignments'. A table at the bottom provides an overview of the components.

Table 1: The SBML components in this model.  
All components are described in more detail in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	4
events	0	constraints	0
reactions	2	function definitions	0
global parameters	0	unit definitions	2
rules	0	initial assignments	0

## 2 Unit Definitions

This is an overview of seven unit definitions. The units substance, volume, area, length, and time are predefined by SBML and not mentioned in the model.

### 2.1 Unit per second

**Definition**  $\text{s}^{-1}$

### 2.2 Unit litre per mole per second

**Definition**  $\text{mol}^{-1} \cdot \text{l} \cdot \text{s}^{-1}$

### 2.3 Unit substance

**Notes** Mole is the predefined SBML unit for substance.

**Definition** mol

### 2.4 Unit volume

**Notes** Litre is the predefined SBML unit for volume.

**Definition** l

### 2.5 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition** m<sup>2</sup>

### 2.6 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

### 2.7 Unit time

**Notes** Second is the predefined SBML unit for time.

**Definition** s

### 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
	cytosol		3	$10^{-14}$	l	gf	

#### 3.1 Compartment cytosol

This is a three-dimensional compartment with a constant size of  $10^{-14}$  litre.

### 4 Species

This model contains four species. Section 6 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
E8	ES	cytosol	$\text{mol} \cdot \text{l}^{-1}$	■	■
P	P	cytosol	$\text{mol} \cdot \text{l}^{-1}$	■	■
S	S	cytosol	$\text{mol} \cdot \text{l}^{-1}$	■	■
E	E	cytosol	$\text{mol} \cdot \text{l}^{-1}$	■	■

### 5 Reactions

This model contains two reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by one or more modifiers, the identifiers of the modifier species are written above the reaction arrow.

Table 4: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	v <sub>eq</sub>		$E + S \rightleftharpoons ES$	
2	v <sub>cat</sub>		$ES \longrightarrow E + P$	

## 5.1 Reaction veg

This is a reversible reaction of two reactants forming one product.

### Reaction equation



### Reactants

Table 5: Properties of each reactant.

Id	Name	SBO
E	E	
S	S	

### Product

Table 6: Properties of each product.

Id	Name	SBO
ES	ES	

### Kinetic Law

Derived unit  $s^{-1} \cdot mol$

$$v_1 = \text{vol(cytosol)} \cdot (k_{on} \cdot [E] \cdot [S] - k_{off} \cdot [ES]) \quad (2)$$

Table 7: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
k <sub>on</sub>			1000000.0	$mol^{-1} \cdot l \cdot s^{-1}$	<input checked="" type="checkbox"/>
k <sub>off</sub>			0.2	$s^{-1}$	<input checked="" type="checkbox"/>

## 6 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

### 6.1 Species ES

Name ES

Initial amount 0 mol

This species takes part in two reactions (as a reactant in  $v_{cat}$  and as a product in  $v_{eq}$ ).

$$\frac{d}{dt} ES = v_1 - v_2 \quad (5)$$

### 6.2 Species P

Name P

Initial amount 0 mol

This species takes part in one reaction (as a product in  $v_{cat}$ ).

$$\frac{d}{dt} P = v_2 \quad (6)$$

### 6.3 Species S

Name S

Initial amount  $10^{-39}$  mol

This species takes part in one reaction (as a reactant in  $v_{eq}$ ).

$$\frac{d}{dt} S = -v_1 \quad (7)$$

### 6.4 Species E

Name E

Initial amount  $5 \cdot 10^{-21}$  mol

This species takes part in two reactions (as a reactant in  $v_{eq}$  and as a product in  $v_{cat}$ ).

$$\frac{d}{dt} E = v_2 - v_1 \quad (8)$$

# es gibt bereits sehr viele Modelle

The screenshot shows the BioModels Database homepage. At the top, there's a header bar with the title "BioModels Database" and a search bar containing the URL "http://www.ebi.ac.uk/biomodels-main/". Below the header is a navigation menu with links for "Databases", "Tools", "EBI Groups", "Training", "Industry", "About Us", "Help", "Site Index", "BioModels Home", "Browse models", "Submit", "Sign in", "Support", and "About BioModels". A "Give us feedback" button is also present. The main content area has a title "BioModels Database - A Database of Annotated Published Models". It includes a brief description of the database, a search bar with "Search", "Go to the model", and "Advanced search" buttons, and a sidebar featuring a "Model of the month" section for May 2009 about sucrose accumulation in sugar cane, followed by a "News" section.

BioModels Database - A Database of Annotated Published Models

BioModels Database is a data resource that allows biologists to store, search and retrieve published mathematical models of biological interests. Models present in BioModels Database are annotated and linked to relevant data resources, such as publications, databases of compounds and pathways, controlled vocabularies, etc.

Search Go to the model Advanced search

**Browse models**

- Curated models (216)
- Browse models using GO
- Non-curated models (196)

**Simulate in JWS Online**

**Submit a model**

Mirror at California Institute of Technology <http://biomodels.caltech.edu>

<http://www.ebi.ac.uk/biomodels-main/modelmonth>

**Model of the month**

May 2009

Sucrose accumulation is accompanied by continuous synthesis and degradation processes in the developing sugar cane, *Saccharum officinarum*. Sugar cane internode maturation coincides with increased sucrose storage, but is not dependent purely on time. In addition, cane varieties accumulate sucrose to quite divergent extents.

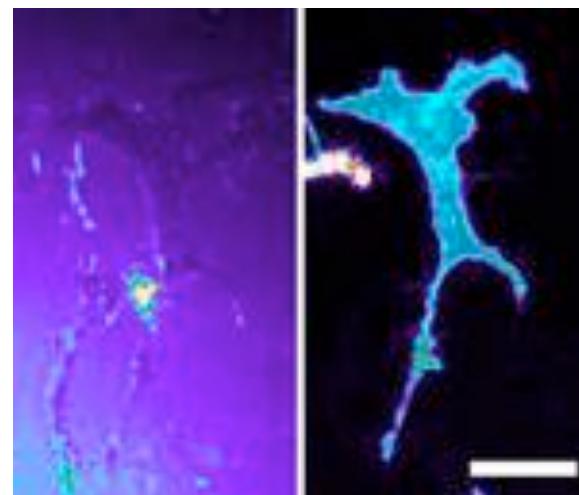
[Read more...](#)

**News**

16th June 2009 Fourteenth release  
[Download All Models Under SBML Format](#)

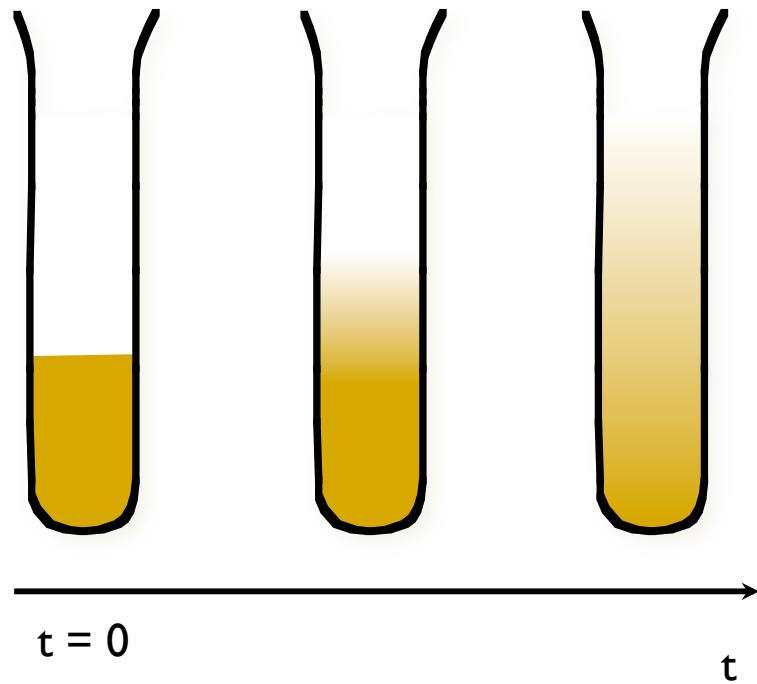
# Prozesse in einer Zelle

Schneider und Haugh "Quantitative elucidation of a distinct spatial gradient-sensing mechanism in fibroblasts", *JCB* **171** (2005) 883



PI 3-kinase signaling in response to a transient PDGF gradient. The video depicts the experiment presented in Fig. 5 A of the paper, with TIRF time courses of the extracellular OG 514-dextran gradient (left) and intracellular CFP-AktPH translocation response (right). A CFP-AktPH-transfected fibroblast was stimulated with a moving PDGF gradient for 21 min, after which a uniform bolus of 10 nM PDGF and subsequently wortmannin were added (additions indicated by the flashing screen). The video plays at 7.5 frames/s (150x speed up). Bar, 30  $\mu$ m.

# Diffusion



Diffusion  
=> verschmiert Unterschiede

Entwicklung der ortsabh. Dichte  
<=> Diffusionsgleichung

$$\rho(\vec{r}, t) = \frac{\Delta N(\vec{r}, t)}{\Delta V}$$

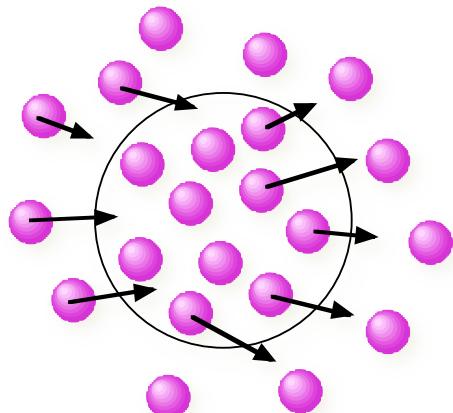
+ ortsabhängige Quellen und Senken

# Kontinuitätsgleichung

Zwei Beiträge zur Diffusionsgleichung:

I) Kontinuitätsgleichung: wo bleibt das Material?

$$\frac{\partial \rho(\vec{r}, t)}{\partial t} = -\nabla \vec{j}(\vec{r}, t) = -\operatorname{div} \vec{j}(\vec{r}, t)$$



Änderung der  
Dichte  $\rho$  bei  $(r, t)$

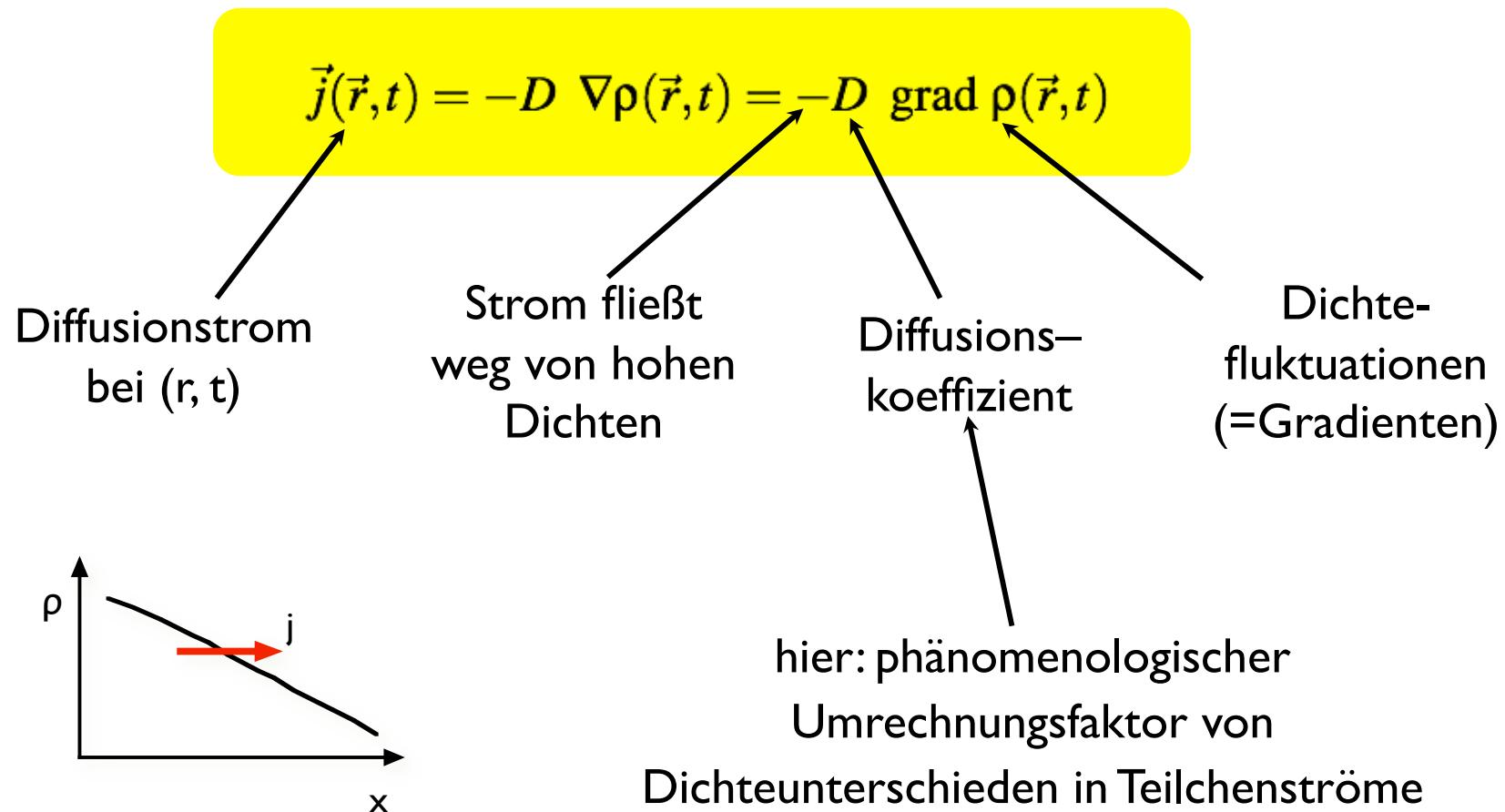
Divergenz des  
Stromes = Quellen und  
Senken für Teilchen

partielle Ableitung:  
=> betrachte nur Änderungen von  $\rho$  in der Zeit an einem  
festgehaltenen Ort  $r$  (nicht: Ortsverschiebungen  $r = r(t)$ )

$$\Delta N = N_{in} - N_{out} = 3 - 5 = -2$$

# Diffusionsstrom

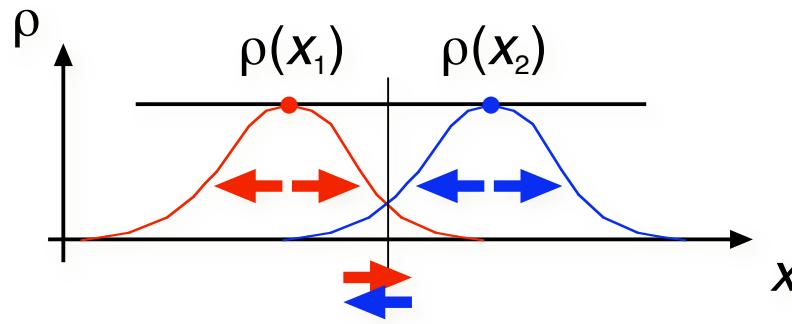
2) Diffusionsstrom durch Dichteunterschiede (Gradienten) – Fick'sches Gesetz:



# Diffusion mikroskopisch

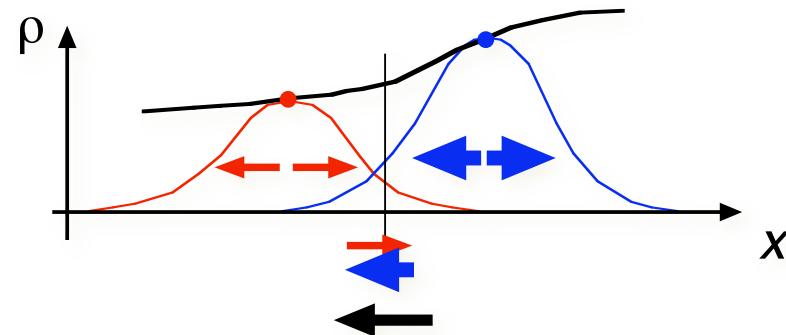
Ohne externe Kräfte

=> Teilchen bewegen sich in alle Richtungen gleich wahrscheinlich  
(Gauss'sche Wahrscheinlichkeit)



$$\rho(x_1) = \rho(x_2) \Rightarrow j_{\text{diff}} = 0$$

$$j_{\text{diff}} \propto -\frac{\rho(x_2) - \rho(x_1)}{x_2 - x_1} \Rightarrow \frac{d\rho}{dx}$$



$$\rho(x_1) < \rho(x_2) \Rightarrow j_{\text{diff}} < 0$$

Gleiche Dichten an  $x_1$  und  $x_2$ :  
=> gleiche Anzahl Teilchen springt  
von  $x_1 \Rightarrow x_2$  wie von  $x_2 \Rightarrow x_1$

Unterschiedliche Dichten:  
=> mehr Teilchen springen  
von  $x_2 \Rightarrow x_1$  als von  $x_1 \Rightarrow x_2$

# Diffusionsgleichung: partielle DGL

Diffusionsstrom

$$\vec{j}(\vec{r}, t) = -D \nabla \rho(\vec{r}, t) = -D \operatorname{grad} \rho(\vec{r}, t)$$

in Kontinuitätsgleichung einsetzen

$$\frac{\partial \rho(\vec{r}, t)}{\partial t} = -\nabla \cdot \vec{j}(\vec{r}, t) = -\operatorname{div} \vec{j}(\vec{r}, t)$$

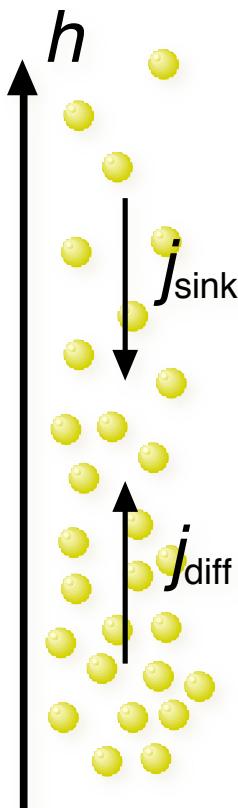
=> Diffusionsgleichung:

$$\frac{\partial \rho(\vec{r}, t)}{\partial t} = -\nabla(-D \nabla \rho(\vec{r}, t)) \stackrel{D(\vec{r}, t) = \text{const}}{=} D \Delta \rho(\vec{r}, t)$$

=> Vollständige Beschreibung der zeitabhängigen Dichteverteilung  
(ohne externe Kräfte)

# Zur Boltzmann-Verteilung

Diffusion unter dem Einfluß einer externen Kraft (z.B. Schwerkraft)  
=> stationäre Lösung der Diffusionsgleichung



**zwei Beiträge**

Gravitation  
=> Moleküle sinken

$$j_{sink}(h) = v \rho(h) = -\frac{mg}{\gamma} \rho(h)$$

Dichteunterschied  
=> Diffusionsstrom

$$j_{diff}(h) = -D \frac{d\rho(h)}{dh}$$

stationärer Zustand:  $j_{sink}(h) + j_{diff}(h) = 0$

Mit  $D = \frac{k_B T}{\gamma}$  =>  $\frac{d\rho(h)}{dh} = -\frac{mg}{k_B T} \rho(h)$

$$\rho(h) = \rho_0 \exp \left[ -\frac{mgh}{k_B T} \right]$$

stationärer Zustand ist unabhängig von  $D$  (aber: Relaxationszeit)

# Integration

Bisher: (System von) ODEs

$$\frac{d}{dt}X_i = f_i(X_1, X_2, \dots)$$

- Zeitentwicklung abhängig von den **lokalen** Werten der Systemparameter
- alle Ableitungen nach der Zeit

Jetzt: Diffusionsgl. mit konstantem D:

$$\frac{\partial \rho(\vec{r}, t)}{\partial t} = D \Delta \rho(\vec{r}, t)$$

- Zeitentwicklung bestimmt durch **globale** Werte (Verteilungen) der Variablen (gesamte Dichte  $\rho(r)$  nötig für Gradient)
- Ableitungen nach **Zeit und Ort**

# FTCS–Integrator

Diffusionsgleichung mit konstantem D in 1D:

$$\frac{\partial \rho(\vec{x}, t)}{\partial t} = D \frac{\partial^2 \rho(\vec{x}, t)}{\partial x^2}$$

Direkte Implementierung auf einem Gitter  $\{\rho(x_i)\}$  mit Abstand  $\Delta x$ :

$$\frac{\rho_j(t + \Delta t) - \rho_j(t)}{\Delta t} = D \frac{\rho_{j+1}(t) - 2\rho_j(t) + \rho_{j-1}(t)}{\Delta x^2}$$

**F**orward in **T**ime

**C**entered in **S**pace

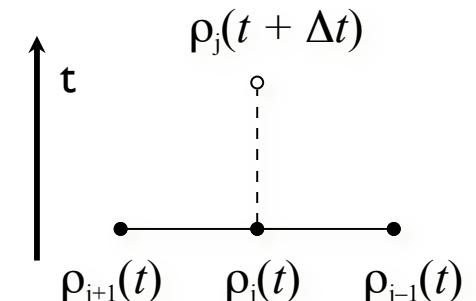
Propagationsschritt:

$$\rho_j(t + \Delta t) = \rho_j(t) + \Delta t D \frac{\rho_{j+1}(t) - 2\rho_j(t) + \rho_{j-1}(t)}{\Delta x^2}$$

Stabil für:

$$\Delta t \leq \frac{\Delta x^2}{2D}$$

( $\Delta t <$  Diffusionszeit über Abstand  $\Delta x$ )

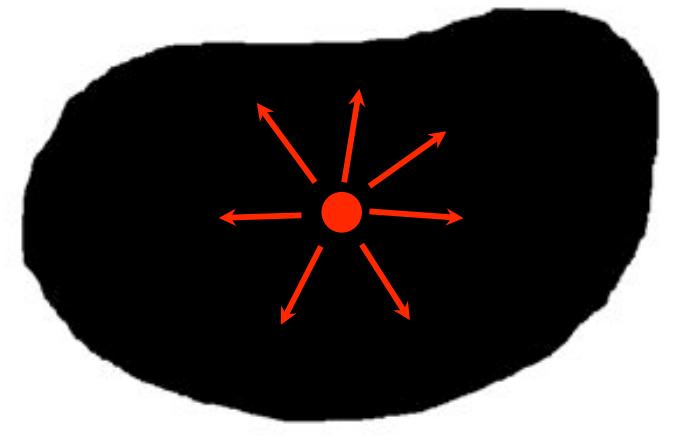
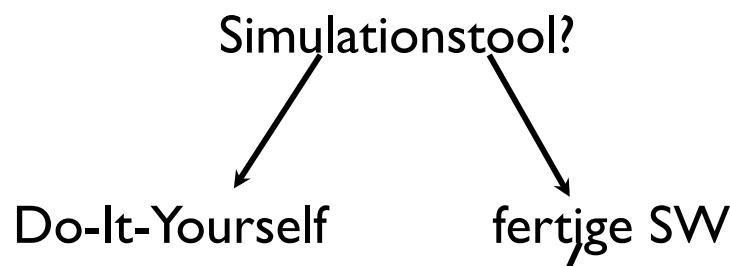


# Beispiel: Diffusion

Moleküle werden bei  $x_s$  produziert und in der ganzen Zelle abgebaut

Diffusion in beliebiger Geometrie:

=> Einfluß der Wände?



"The Virtual Cell":

- Reaktions-Diffusions-Systeme
- kontinuierliche und stochastische Integration
- frei definierbare Geometrien (Fotos)
- lokales Java-Frontend + Cluster @ NRCAM

Running the Virtual Cell and User Information

http://www.nrcam.uchc.edu/login/login.html

Google Python Tutorial Python Library Reference Vesilweb@develop Vesilweb@service Molecular Systems Biology QTVYouTube

# National Resource for Cell Analysis and Modeling

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**VCell Login**  
Run the Virtual Cell.

**Virtual Cell User Documentation**

User Guide, Quick Start and Tutorials

**Release Notes**

Current information on Release and Beta versions.

**Technical Requirements**

Hardware and software system specific requirements.

## Run the Virtual Cell

### Release and Beta Versions

The Virtual Cell requires Java. [Get It Now](#)

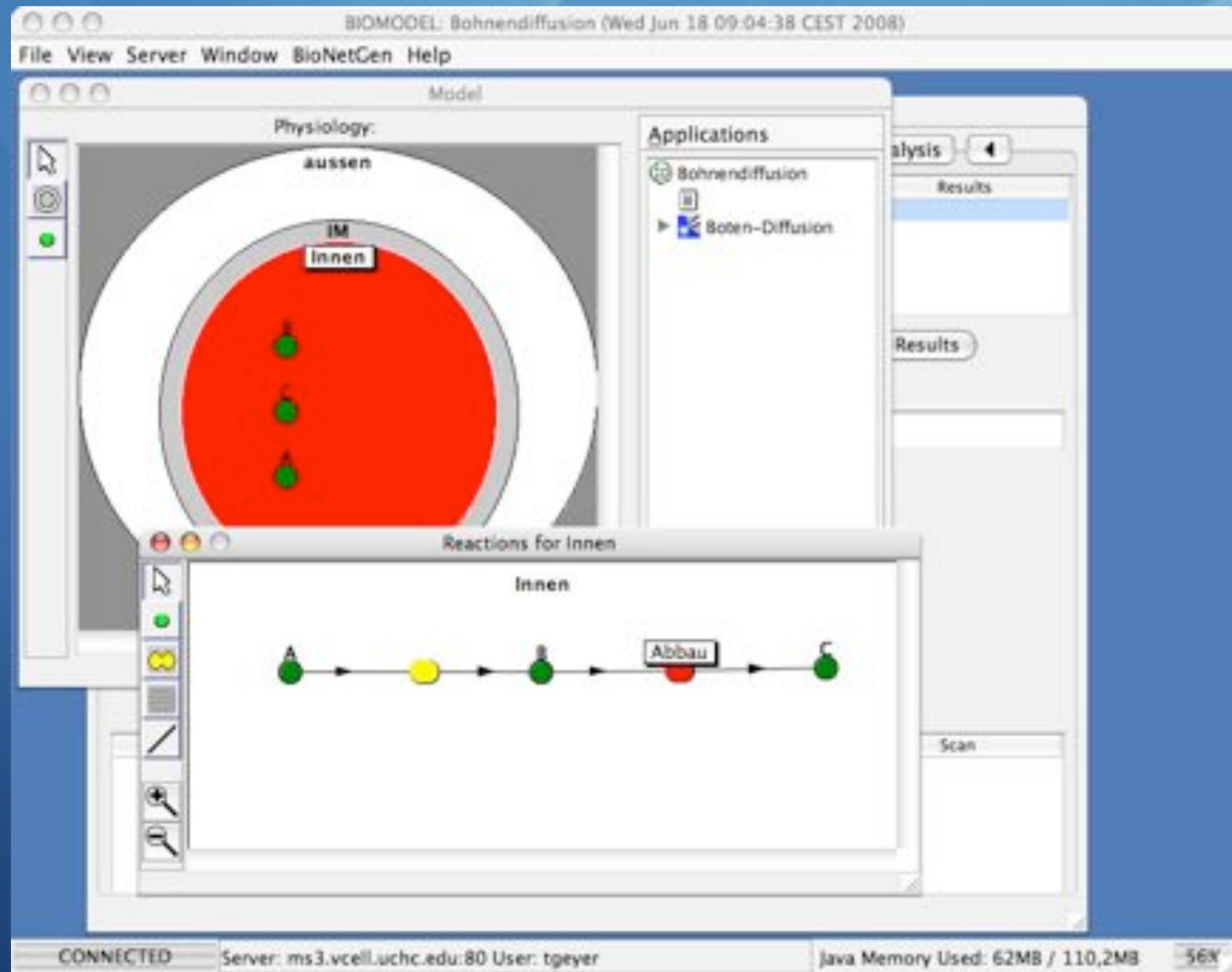
### Run VCell 4.4

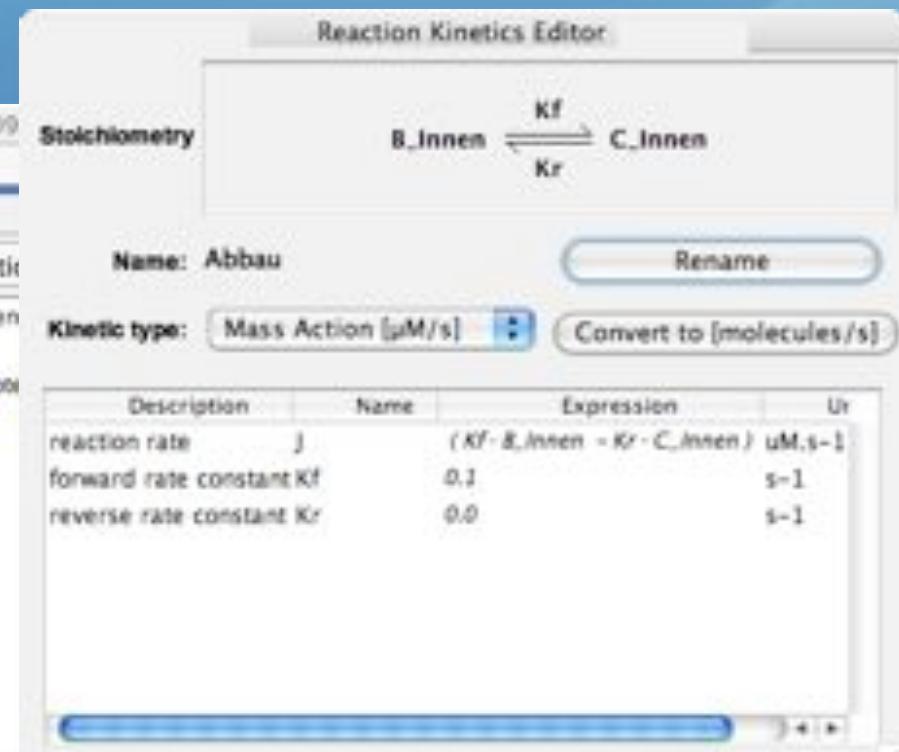
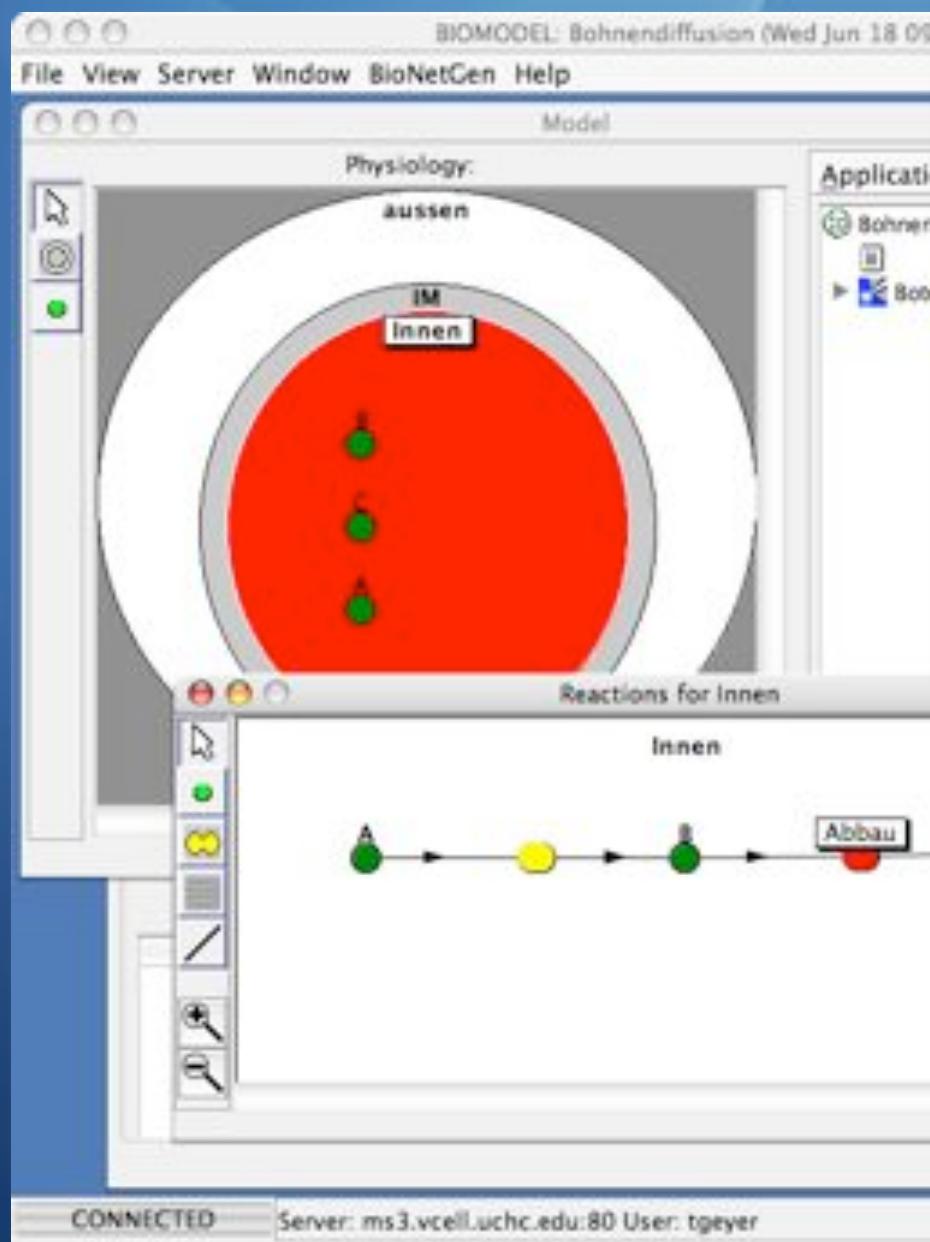
(Please Note: New Users will need to register when they first run the Virtual Cell Software.)

### New Features in 4.4

- [nonspatial stochastic modeling](#)
- field data (using Images data as input to simulations)
- annotations (MIRIAM compliant)
- better SBML support

**download and run  
a Java frontend**





BIOMODEL: Bohnendiffusion (Wed Jun 18 09:04:38 CEST 2008)

File View Server Window BioNetGen Help

APPLICATION: Boten-Diffusion

Reaction Mapping Electrical Mapping View Math Simulation Analysis

Name	Last saved	Running status	Results
Lauf1	Wed Jun 18 09:04:38 CEST 2008	36%	yes

New Edit Copy Delete Run Stop Results

SIMULATION SUMMARY:

Comments:

Spatial: yes

Time: start end timestep output  
0.0 250.0 0.1 keep every 10

Sensitivity: no analysis

Solver: Finite Volume, Regular Grid

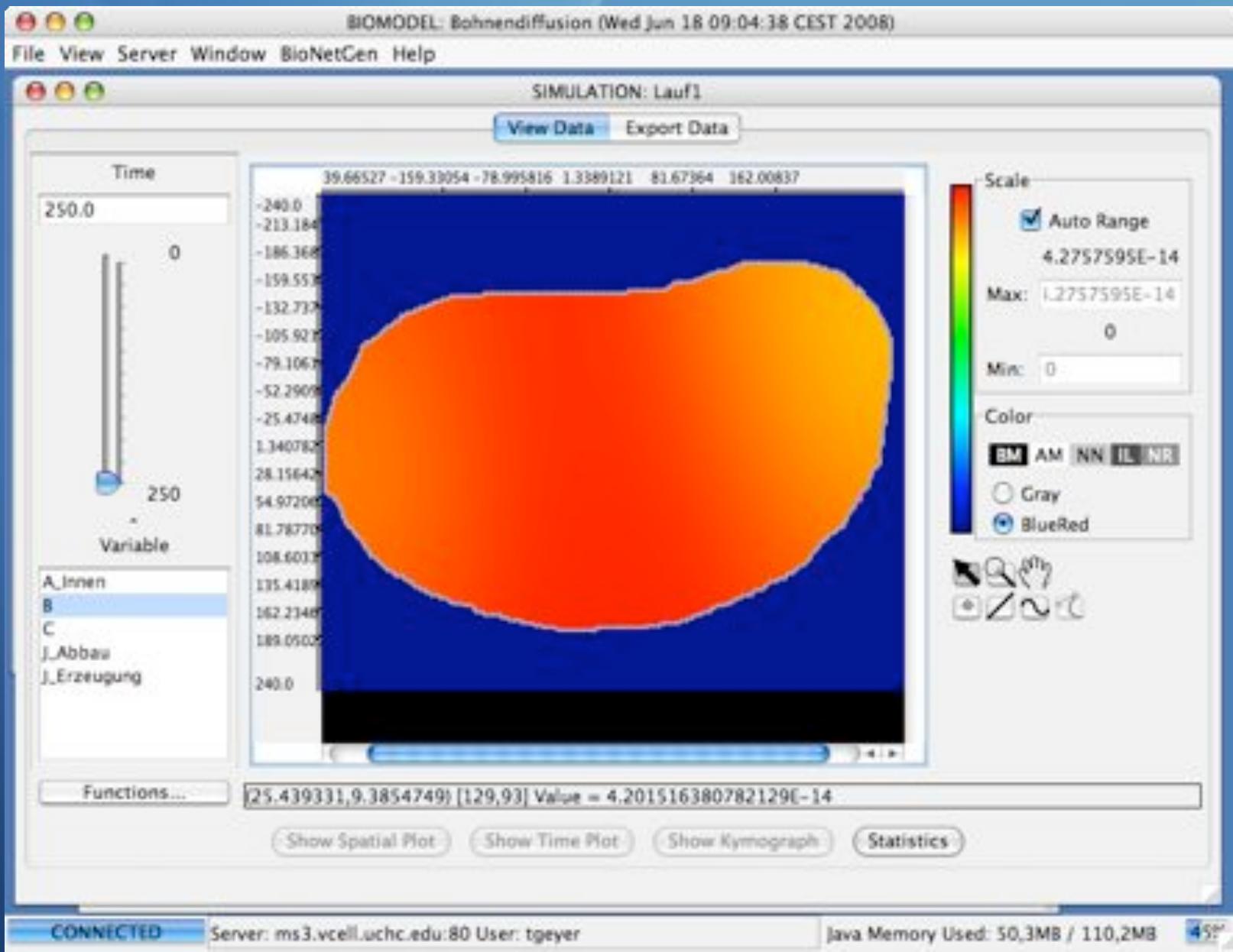
Geometry size: (640.0,480.0) microns

Mesh: 240 x 180 = 43200 elements

Parameters with values changed from defaults:

Parameter Name	Default Value	Change Value	Scan

CONNECTED Server: ms3.vcell.uchc.edu:80 User: tgeyer Java Memory Used: 51MB / 109,6MB 46%



CONNECTED

Server: ms3.vcell.uchc.edu:80 User: tgeyer

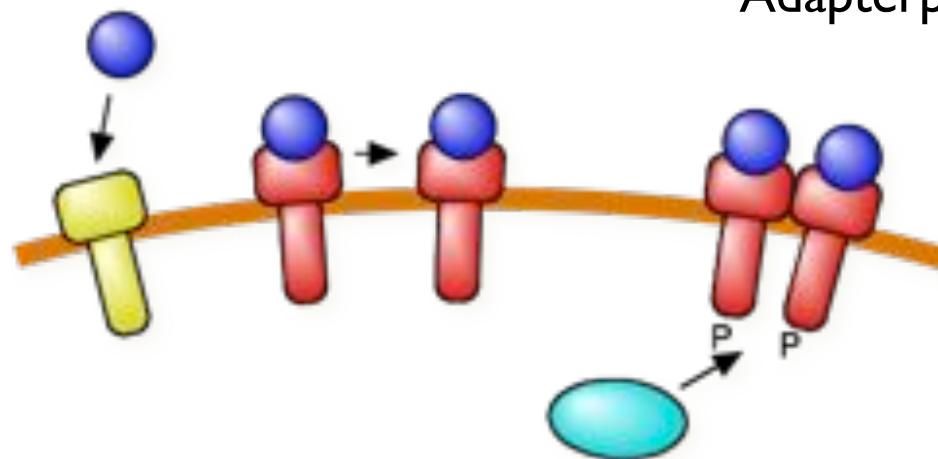
Java Memory Used: 50,3MB / 110,2MB

45°

# Kombinatorische Komplexität

Einfaches Modellsystem:

- externer monovalenter Ligand
- monovalente Rezeptor-Kinase
- Adapterprotein im Zytosol



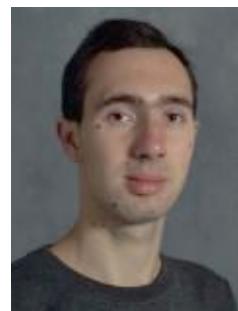
Reaktionen:

- Rezeptor + Ligand
- Rezeptor-Dimere
- Phosphorylierung des Rezeptors
- Bindung des Adapterproteins

3 Spezies + 5 Regeln => 14 Kombinationen im Modell

BioNetGen: Regelbasierter "Biological Network Generator"

# BioNetGen



J. R. Faeder, M. L. Blinov, and W. S. Hlavacek. "Rule-Based Modeling of Biochemical Systems with BioNetGen." In Methods in Molecular Biology: Systems Biology, Ed. I.V. Maly, Humana Press, Totowa, NJ, 2009



BioNetGen@VirtualCell

# toy1.bngl

```

begin parameters
 1 L0 1
 2 R0 1
 3 A0 5
 4 kp1 0.5
 5 km1 0.1
 6 kp2 1.1
 7 km2 0.1
 8 p1 10
 9 d1 5
10 kpA 1e1
11 kmA 0.02
end parameters

begin species
 1 L(r)    L0 # Ligand has one site for binding to receptor.
                 # L0 is initial concentration
 2 R(l,d,Y~U) R0 # Dimer has three sites: l for binding to a ligand,
                   # d for binding to another receptor, and
                   # Y - tyrosine. Initially Y is unphosphorylated, Y~U.
 3 A(SH2)   A0 # A has a single SH2 domain that binds phosphotyrosine
end species

begin reaction rules
# Ligand binding (L+R)
# Note: specifying r in R here means that the r component must not
#       be bound. This prevents dissociation of ligand from R
#       when R is in a dimer.
 1 L(r) + R(l,d) <-> L(r!1).R(l!1,d) kp1, km1

# Aggregation (R-L + R-L)
# Note: R must be bound to ligand to dimerize.
 2 R(l!+,d) + R(l!+,d) <-> R(l!+,d!2).R(l!+,d!2) kp2, km2

# Transphosphorylation
# Note: R must be bound to another R to be transphosphorylated.
 3 R(d!+,Y~U) -> R(d!+,Y~P) p1

# Dephosphorylation
# Note: R can be in any complex, but tyrosine is not protected by bound A.
 4 R(Y~P) -> R(Y~U) d1

# Adaptor binding phosphotyrosine (reversible).
# Note: Doesn't depend on whether R is bound to
#       receptor, i.e. binding rate is same whether R is a monomer, is
#       in association with a ligand, in a dimer, or in a complex.
 5 R(Y~P) + A(SH2) <-> R(Y~P!1).A(SH2!1) kpA, kmA
end reaction rules

begin observables
 Molecules R_dim R(d!+)    # All receptors in dimer
 Molecules R_phos R(Y~P!?)  # Total of all phosphotyrosines
 Molecules A_R  A(SH2!1).R(Y~P!1) # Total of all A's associated with phosphotyrosines
 Molecules A_tot A()        # Total of A. Should be a constant during simulation.
 Molecules R_tot R()        # Total of R. Should be a constant during simulation.
 Molecules L_tot L()        # Total of L. Should be a constant during simulation.
end observables

generate_network();
writeSBML();
simulate_ode({t_end=>50,n_steps=>20});

```

## BioNetGen-Input für das Rezeptor-System von S 35

# Zusammenfassung

SBML:

- hierarchisches XML-Schema
- es gibt viel Software, die SBML lesen und schreiben kann

Diffusion:

- Diffusionsgleichung
- Simulation mit "The Virtual Cell" im Tutorial nächste Woche

Kombinatorische Komplexität

- BioNetGen